

Velocity Images

- the MR

Phase Contrast Technique

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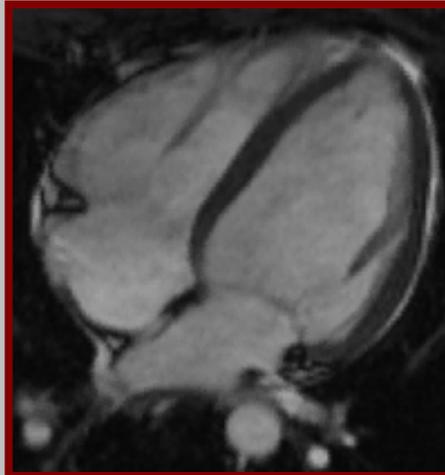
²Siemens AG, Medical Solutions

Introduction

Trend in medical imaging: **From morphology to function.**



„static“



„dynamic“

- Tissue movement
- Fluid flow
- Perfusion
- Diffusion
- Oxygenization and brain activation
- Metabolism

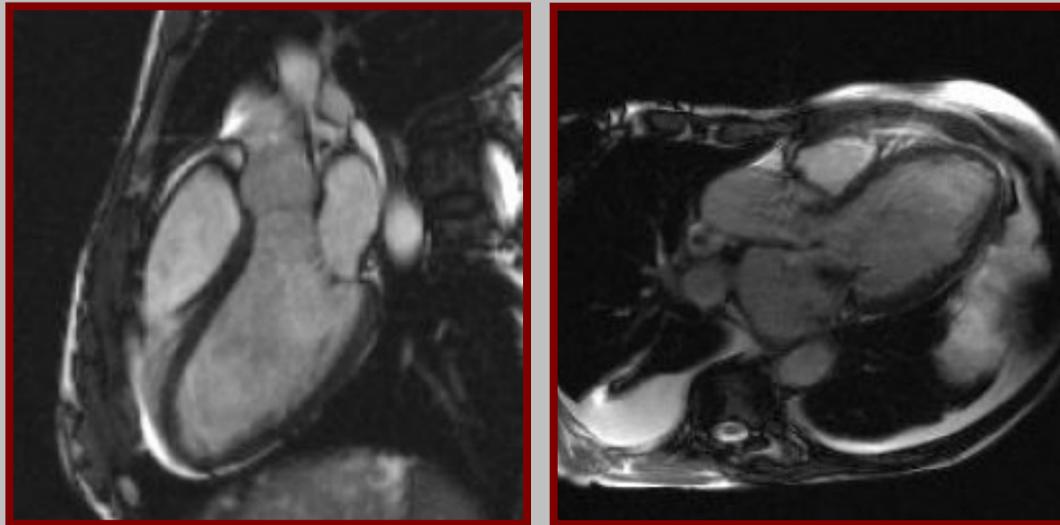
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Introduction

Basic „macroscopic“ variables: **Position \mathbf{x}** („morphology“) and **velocity \mathbf{v}** („dynamics“).

MR imaging generally **motion sensitive**.

Blood flows through mitral valve directed apically, then turns around and flows through aortic valve.



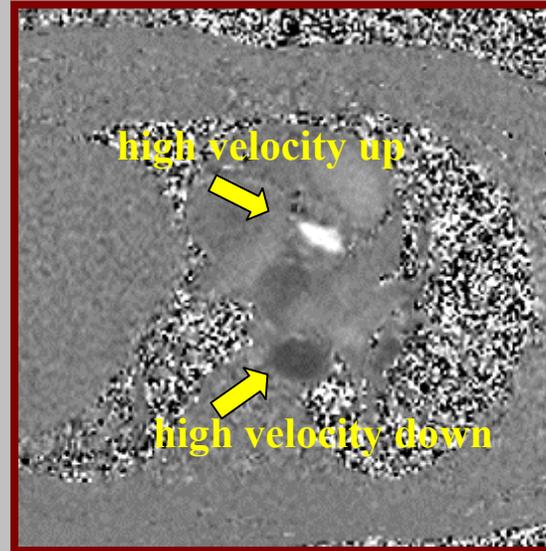
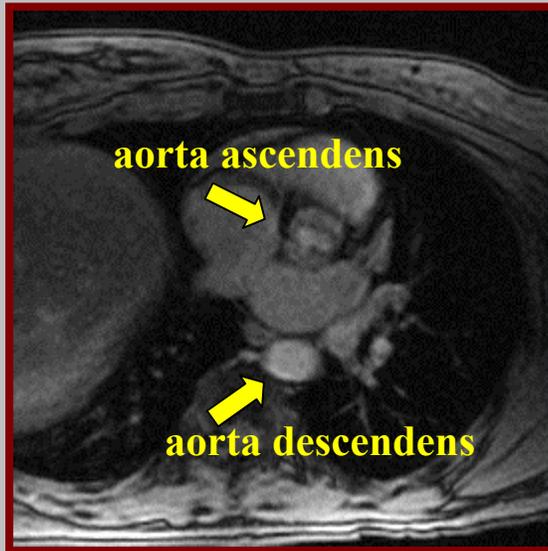
Turbulences (dark) at the mitral and aortic valve

„Qualitative“ blood flow in the heart

Introduction

But **MR** via **phase contrast technique** can even produce pairs of images displaying morphology and velocity.

anatomy

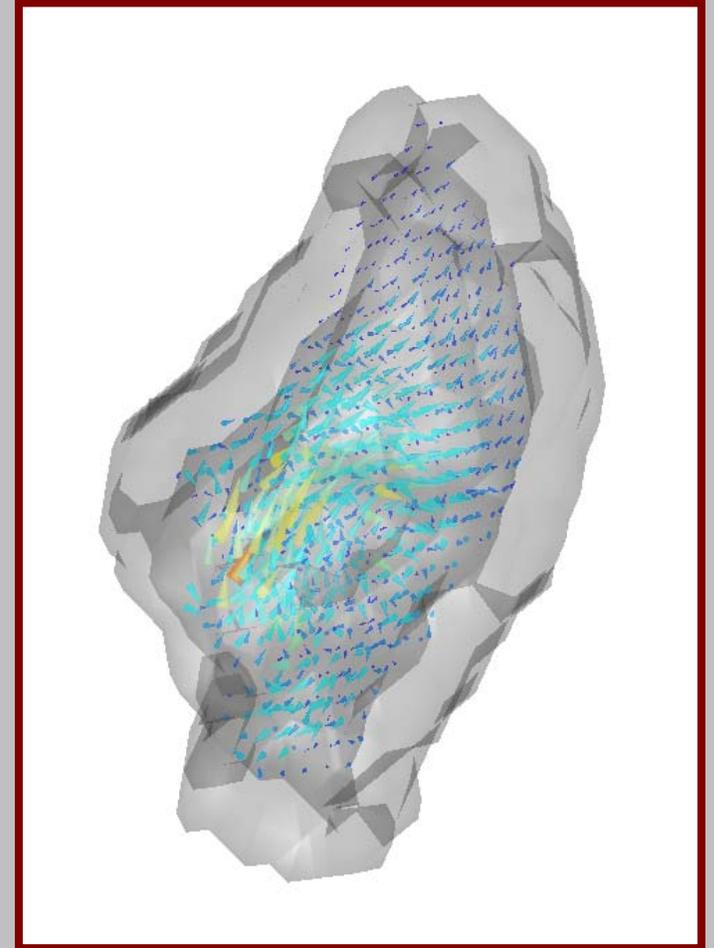


velocity \propto
gray scale

same tomographic slice

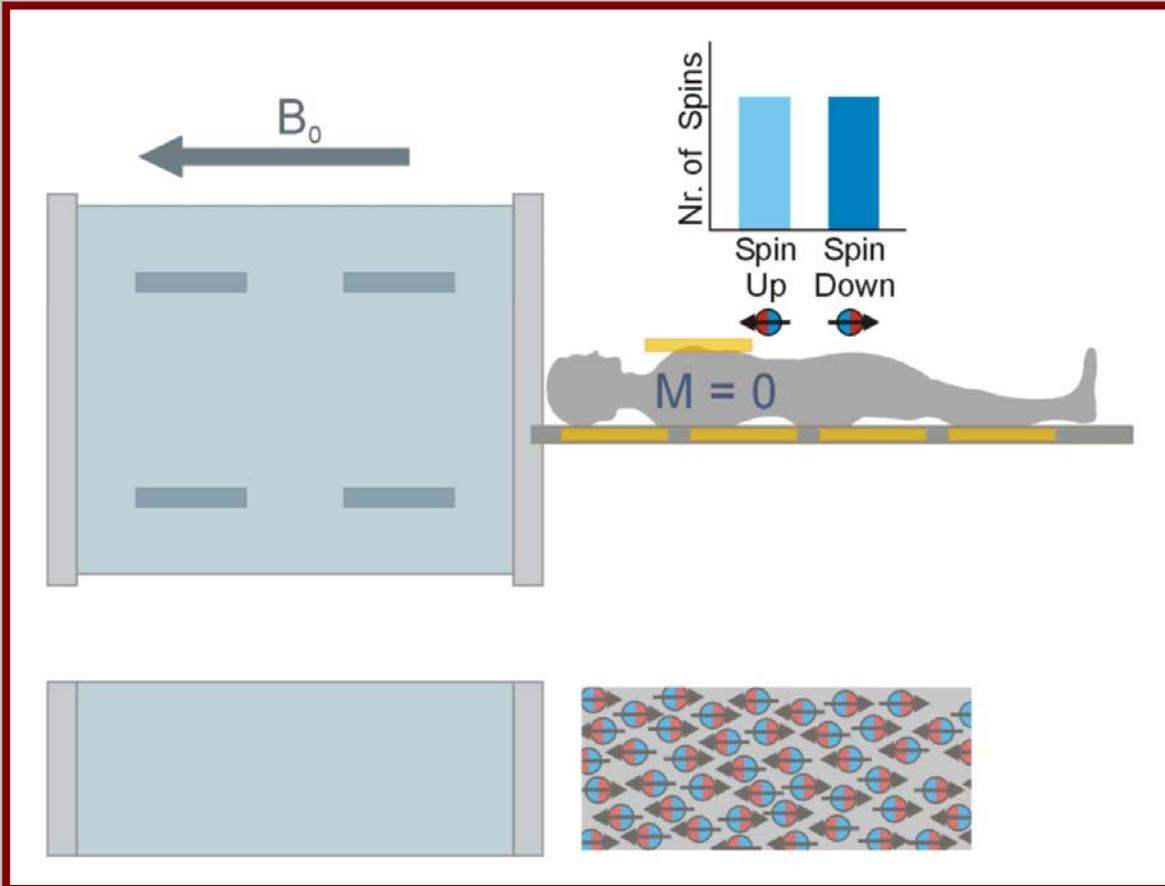
Introduction

- Idea of phase contrast method
- Pulsatility
- Archetypical postprocessing
- Advanced Considerations
- Application examples
- Perspectives



Phase contrast method

Introducing the notion of phase – MR in a nutshell

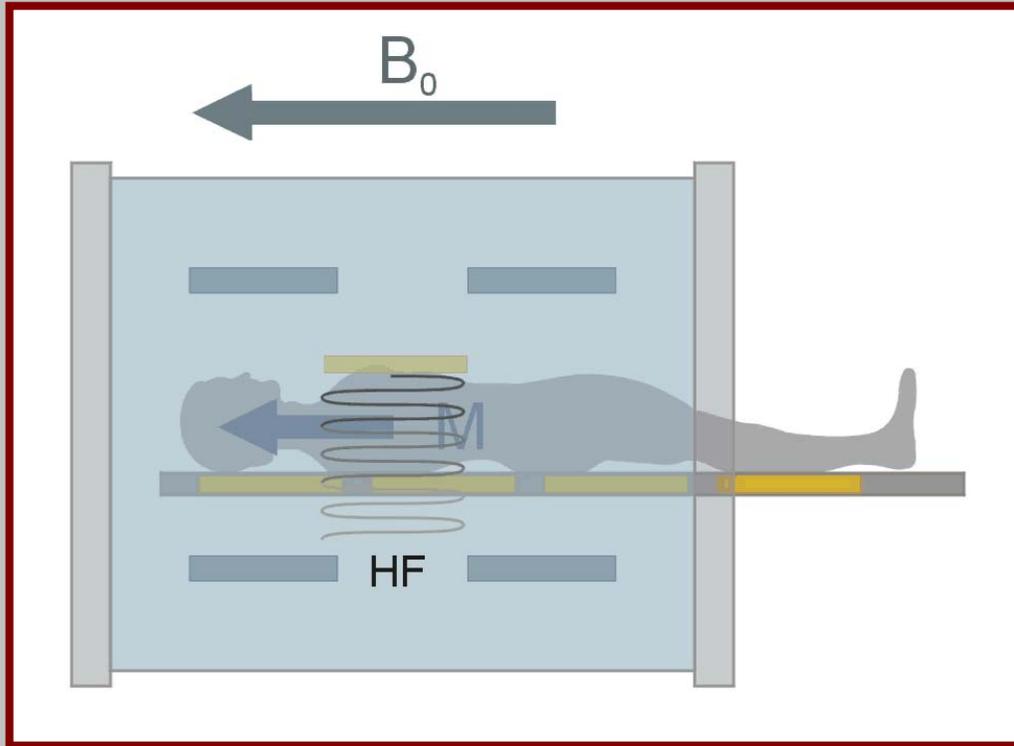


Hydrogen nuclei possess spin (are small magnets).

Static magnetic field B_0 :
Creation of net magnetization M

Phase contrast method

Introducing the notion of phase – MR in a nutshell



Electromagnetic waves at
at **Lamor frequency (HF)**

$$\omega_0 = \gamma B_0$$

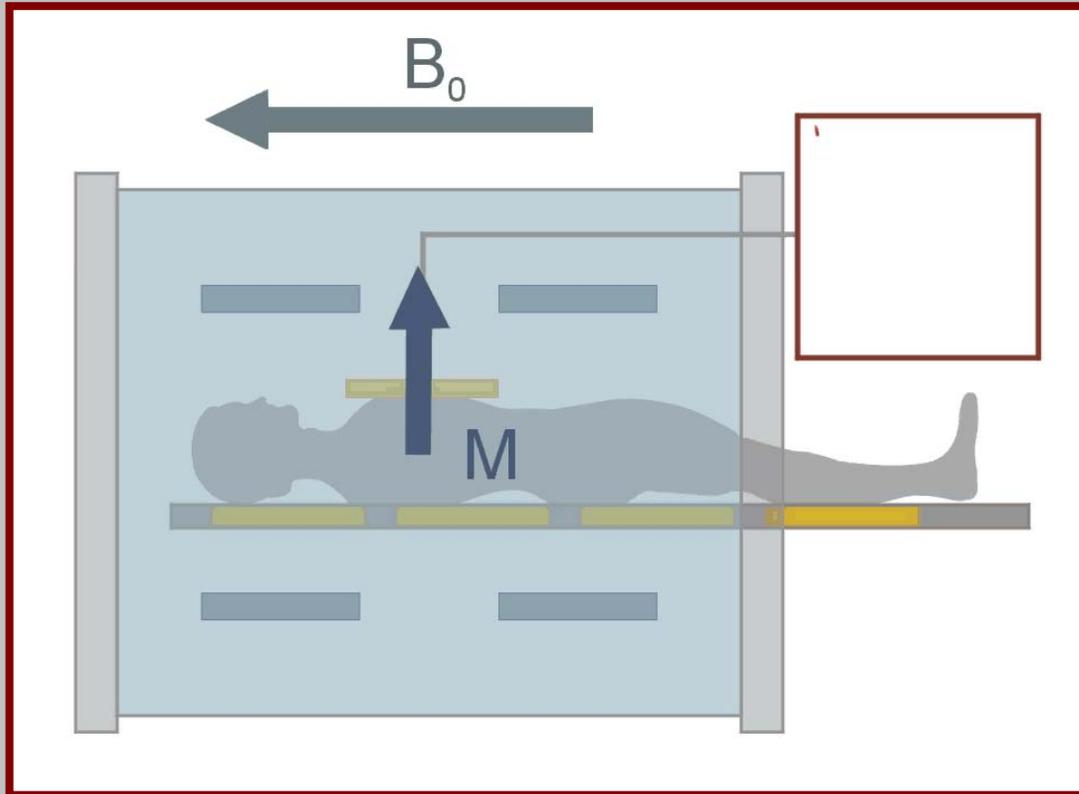
with γ gyromagnetic ratio.

➔ spins flip (**resonance**).

➔ net magnetization
rotates away with ω_0 .

Phase contrast method

Introducing the notion of phase – MR in a nutshell



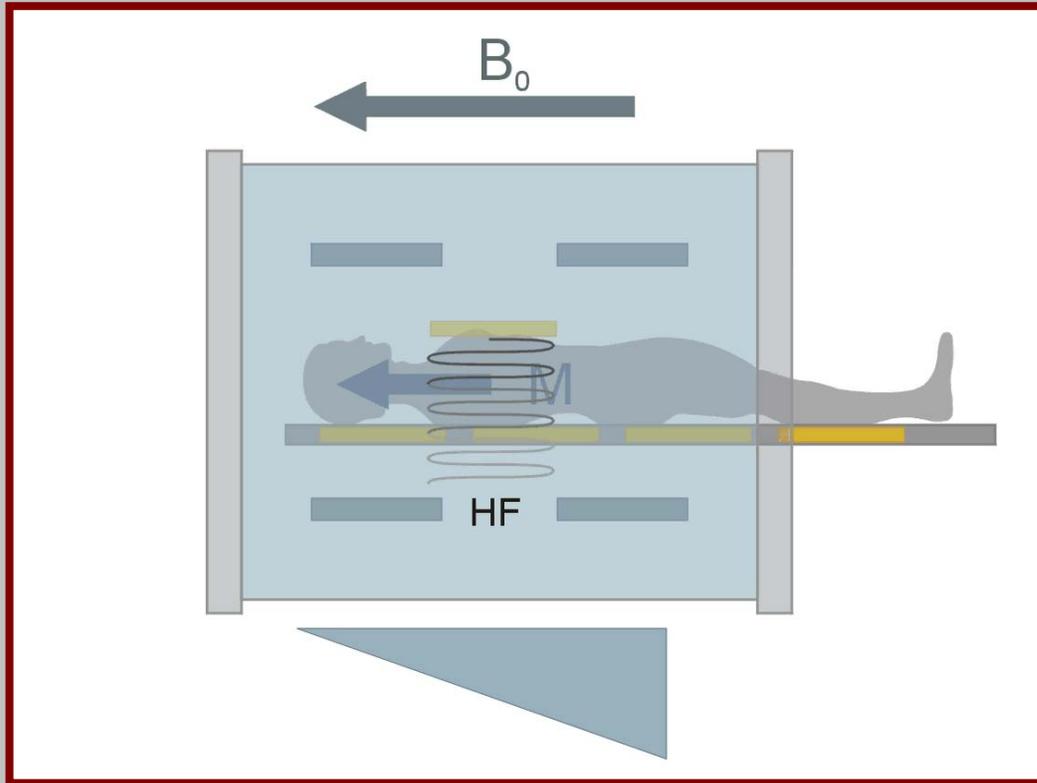
After excitation
magnetization relaxes.

➔ **Transversal** (to B_0)
magnetization M_{\perp} **induces**
signal in coil:

signal $\propto M_{\perp}$

Phase contrast method

Introducing the notion of phase – MR in a nutshell



Gradient magnetic fields

$\mathbf{B}_g \parallel \mathbf{B}_0$:

$$\mathbf{B}_g(\mathbf{r}, t) = \nabla B_g(t) \mathbf{r} = \mathbf{G}(t) \mathbf{r}$$

➔ **Localization** via spatial dependence of angular frequency:

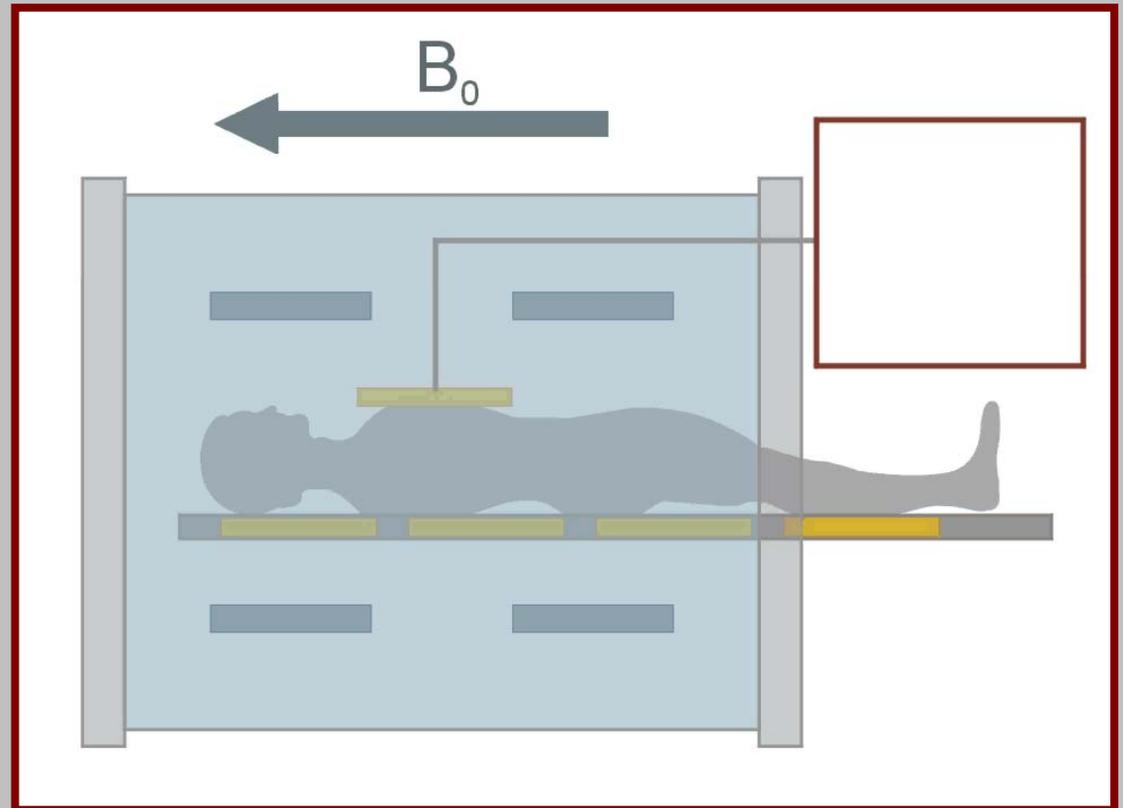
$$\omega(\mathbf{r}, t) = \omega_0 + \gamma \mathbf{G}(t) \mathbf{r}$$

Phase contrast method

Introducing the notion of phase – MR in a nutshell

Signal after „simple“ HF excitation (free induction decay)
not used for imaging.

➔ **Echos**,
after HF pulses and
gradient pulses



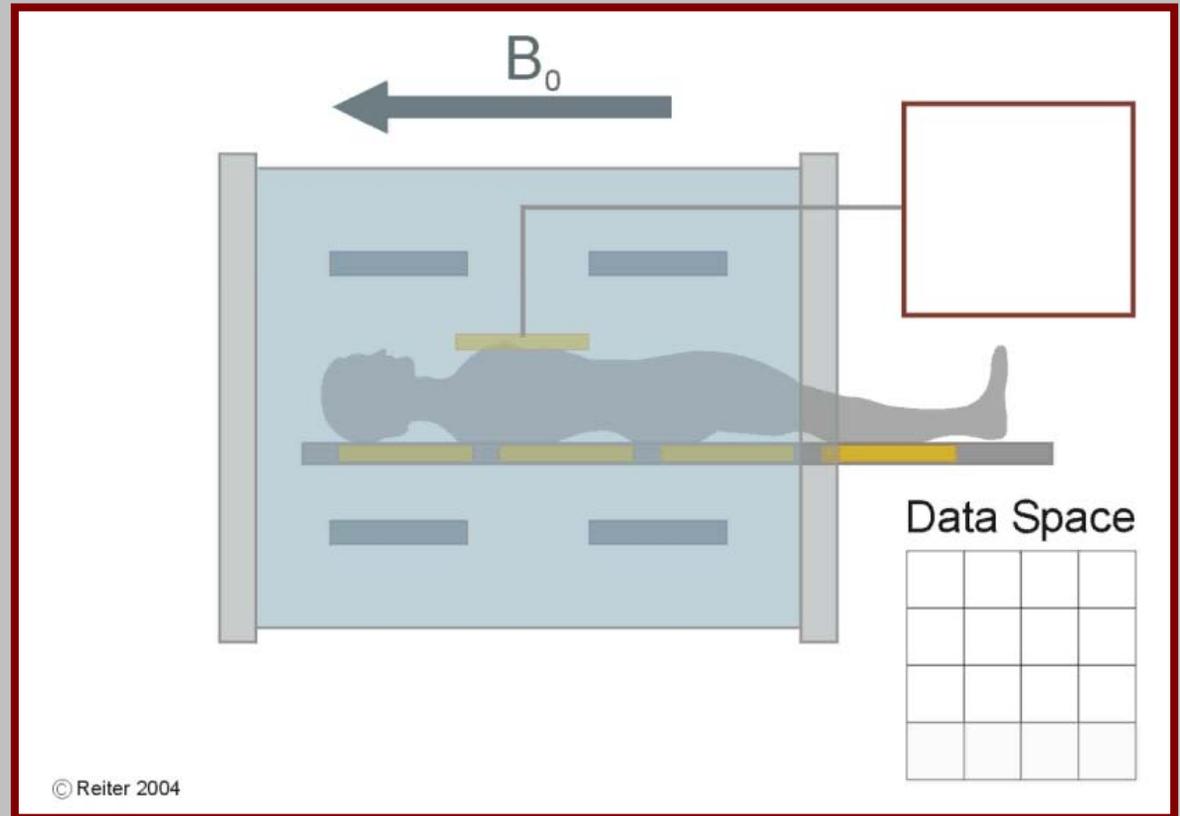
Phase contrast method

Introducing the notion of phase – MR in a nutshell

Echos with different „encoding“ ($\omega(\mathbf{r},t)$) used to fill **data space**.

➔ **Sequence** of HF and gradient pulses:

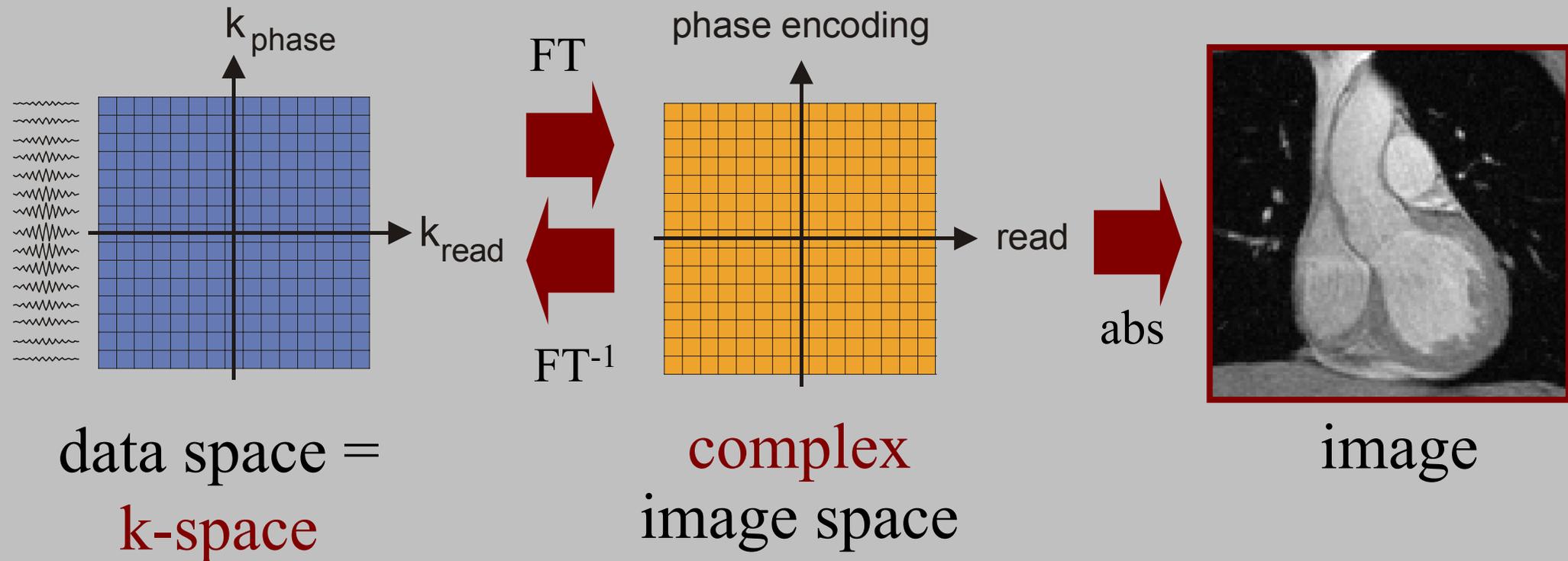
echo \triangleq data line



Phase contrast method

Introducing the notion of phase – MR in a nutshell

Data space and image space connected via **Fourier transform**.

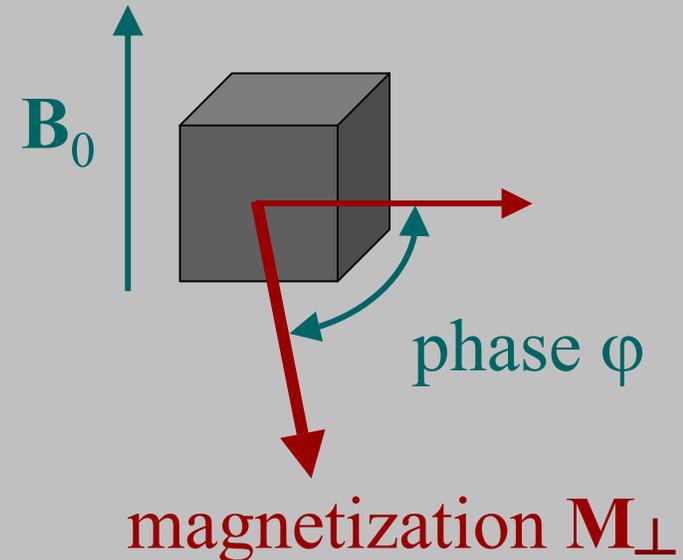


Phase contrast method

Introducing the notion of phase – MR in a nutshell

Pixels represent essentially transversal magnetization of corresponding voxels.

- ➔ **magnitude** M_{\perp}
(seen via abs)
- ➔ **phase** φ of M_{\perp} ,
(at echo time T_E or in a
with ω_0 rotating
coordinate system)

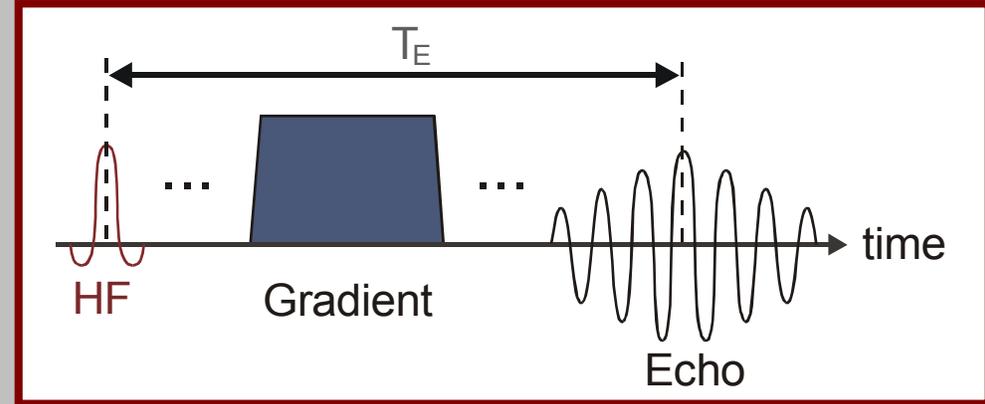


Phase contrast method

Gradients, phase and velocity

Application of a **gradient** changes rotational frequency by:

$$\omega_g(\mathbf{r}, t) = \gamma \mathbf{G}(t) \mathbf{r}$$



Assume tissue is **moving**: $\mathbf{r}(t) = \mathbf{r}(0) + \mathbf{v}(0)t + O(t^2)$

➔ Additional **phase**:

$$\varphi = \int_0^{T_E} dt \omega_g(\mathbf{r}, t) = \gamma \mathbf{r}(0) \int_0^{T_E} dt \mathbf{G}(t) + \gamma \mathbf{v}(0) \int_0^{T_E} dt t \mathbf{G}(t) \boxed{+ O(t^2)} \approx 0$$

Phase contrast method

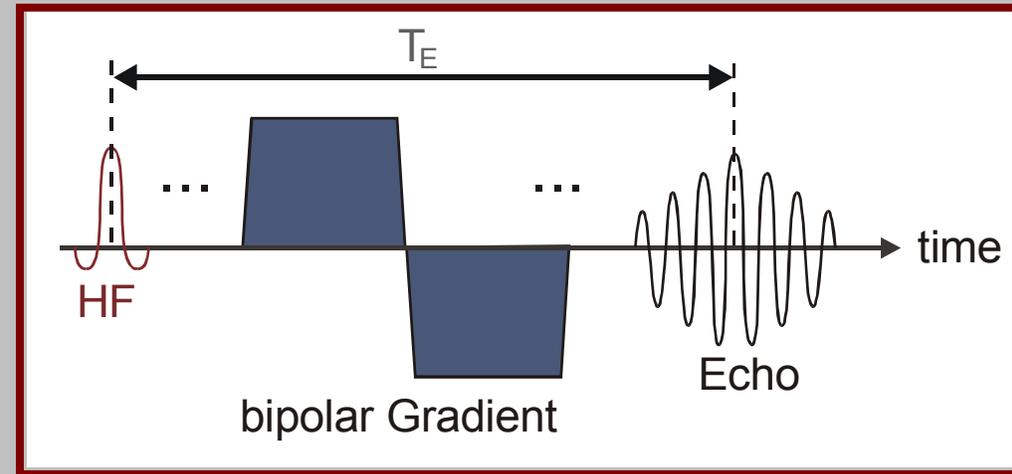
Bipolar gradients

Specifically **bipolar gradient**.

➔ $\mathbf{m}_0 = \int_0^{T_E} dt \mathbf{G}(t) = 0$

➔ **Phase proportional to velocity:**

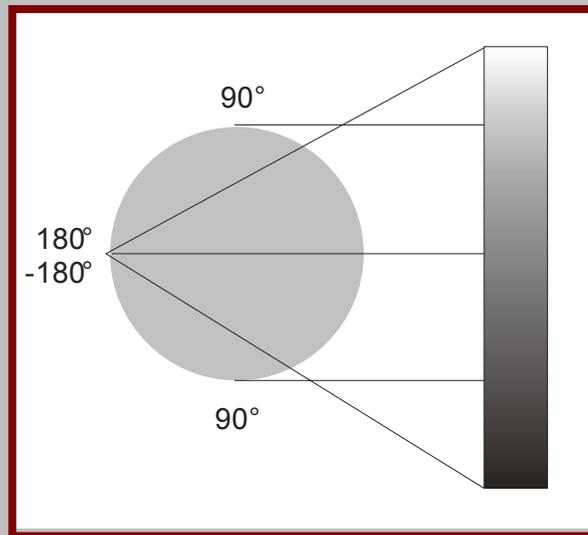
$$\varphi = \gamma \mathbf{v}(0) \mathbf{m}_1 \quad \mathbf{m}_1 = \int_0^{T_E} dt t \mathbf{G}(t)$$



Phase contrast method

Bipolar gradients

First idea: Sequence with bipolar gradient in some direction and **map phase to gray scale**.

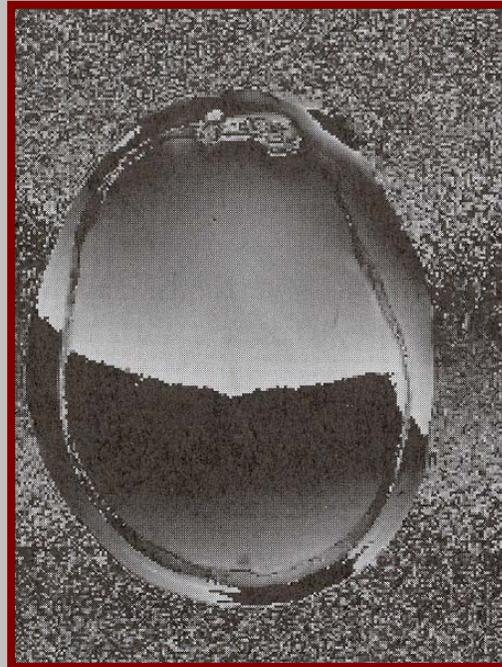


➔ Should give distribution of velocities in this direction.

Phase contrast method

Bipolar gradients

But: **Many reasons for phase changes** of transversal magnetization.



Phase images of the brain: B_0 (and consequently ω_0) is slightly changed by tissue, causing phase changes. Right image is a consequence of an additional small data acquisition error. (Taken from: Haacke EM, et al. Magnetic Resonance Imaging. Wiley, 1999.)

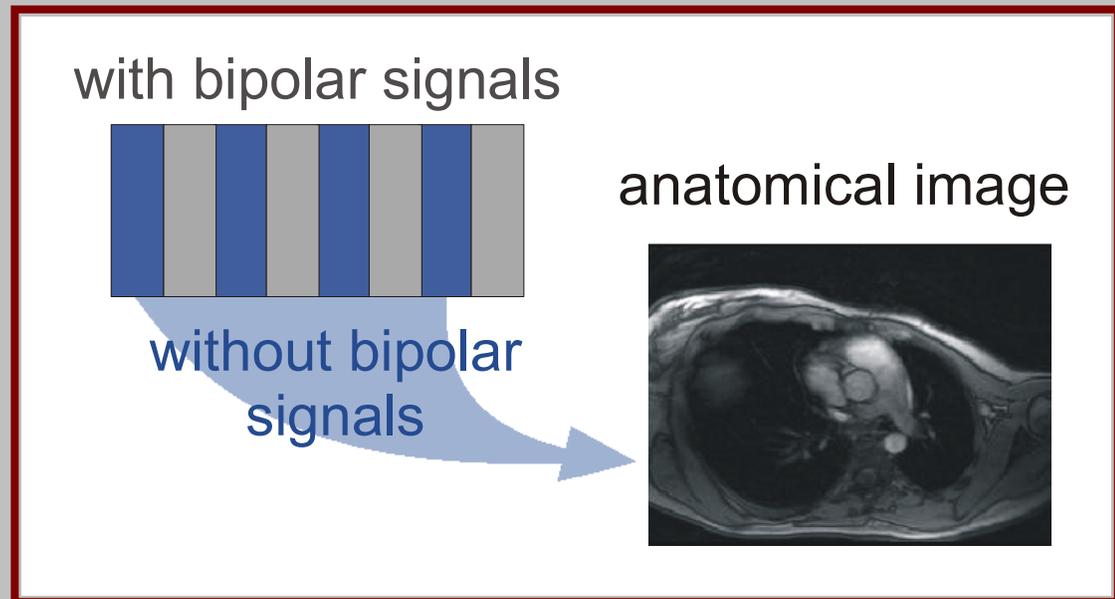
Phase contrast method

Subtraction

Phase contrast method: Measure echos (data lines) twice

- without bipolar gradient
- with bipolar gradient

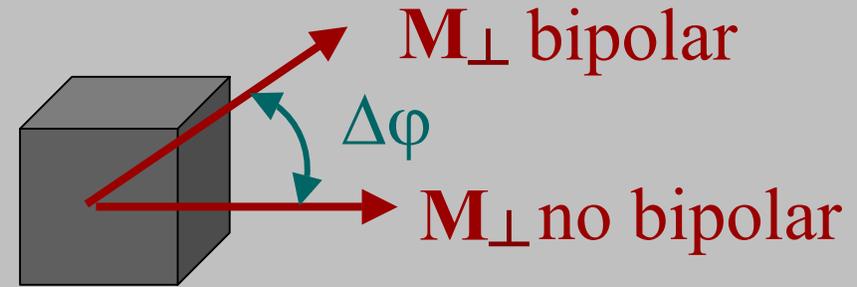
➔ **Anatomical image:**



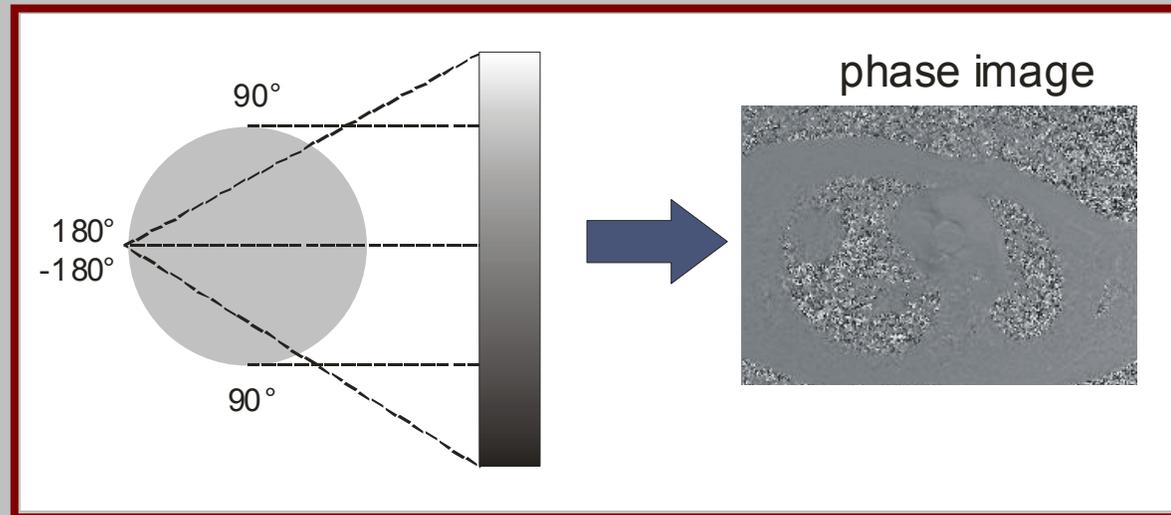
Phase contrast method

Subtraction

➔ Phase or velocity image:



$$\Delta\varphi = \gamma\mathbf{v}(0)\mathbf{m}_1$$

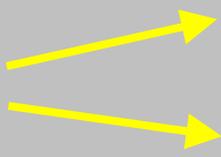


Phase contrast method

Velocity encoding and aliasing

Amount of phase difference caused by velocity determined by first order moments of bipolar gradients:

$$\Delta\varphi = \gamma\mathbf{v}(0)\mathbf{m}_1$$

 m_1 small, large velocities give small phases
 m_1 large, small velocities give large phases

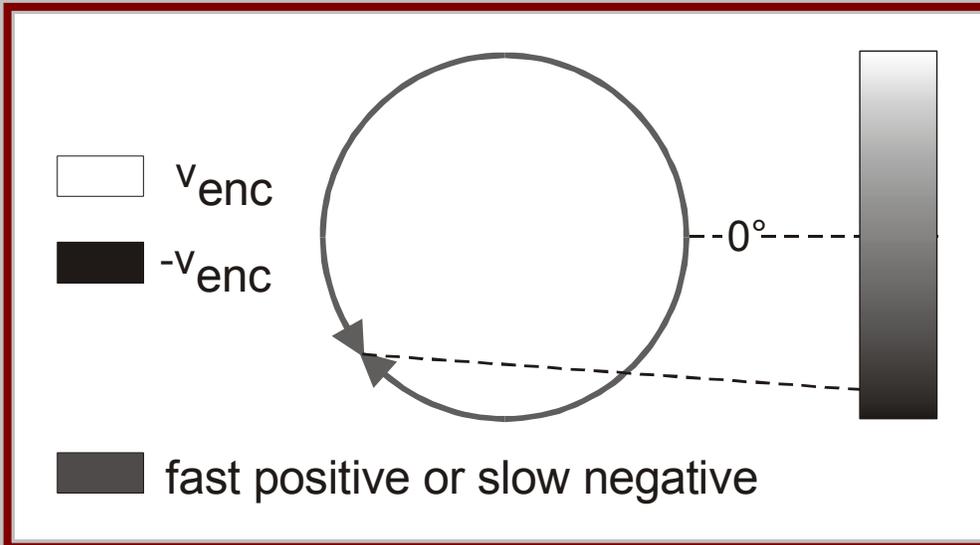
Specify for measurement:

- **Velocity encoding:** $v_{\text{enc}} = \text{velocity for } \Delta\varphi = \pi$
- **Direction** of velocity encoding, typically through-plane

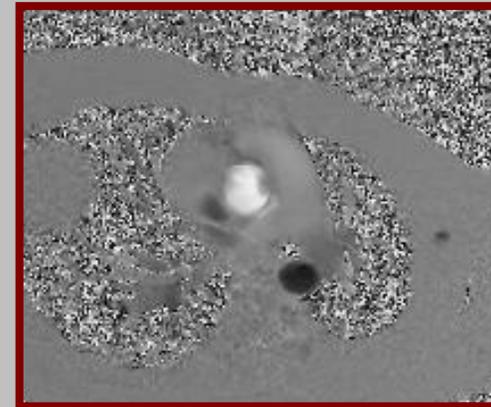
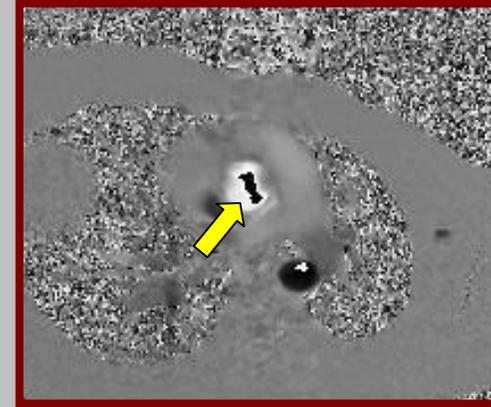
Phase contrast method

Velocity encoding and aliasing

Peculiarity of phase imaging: **Aliasing**



choice of v_{enc}



Correction by assumptions.

Phase contrast method

Noise

Signal-to-noise ratio of phase contrast images:

$$\text{SNR}_v = \frac{\pi}{\sqrt{2}} \frac{v}{v_{\text{enc}}} \text{SNR}_{\text{anat}}$$

➔ Consequence 1 ($\propto 1/v_{\text{enc}}$):

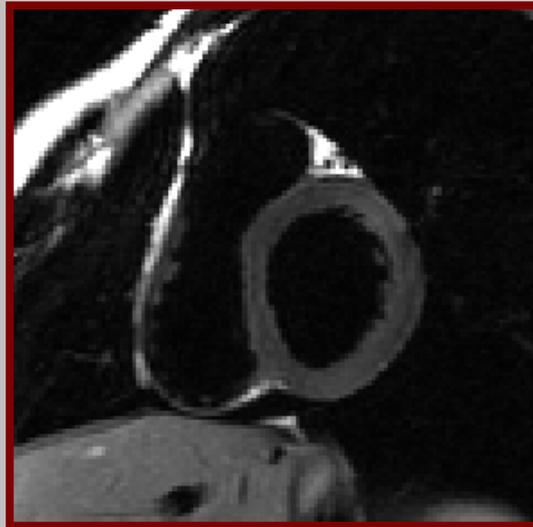
- v_{enc} as small as possible (keeping aliasing small)
- small velocities noisy

Phase contrast method

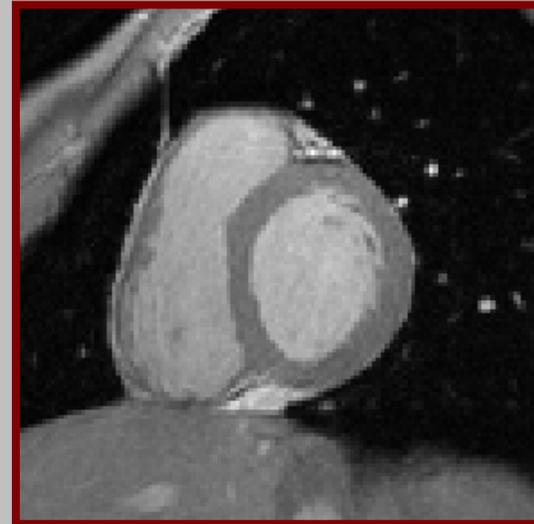
Noise

➔ Consequence 2 ($\propto \text{SNR}_{\text{anat}}$):

Spin echo
sequence:
Blood **dark**
(additionally
slowly)



Gradient echo
sequence:
Blood **bright**
(additionally
fast)



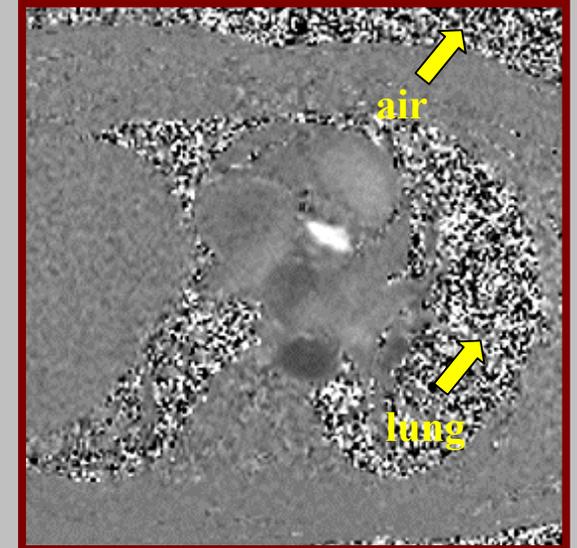
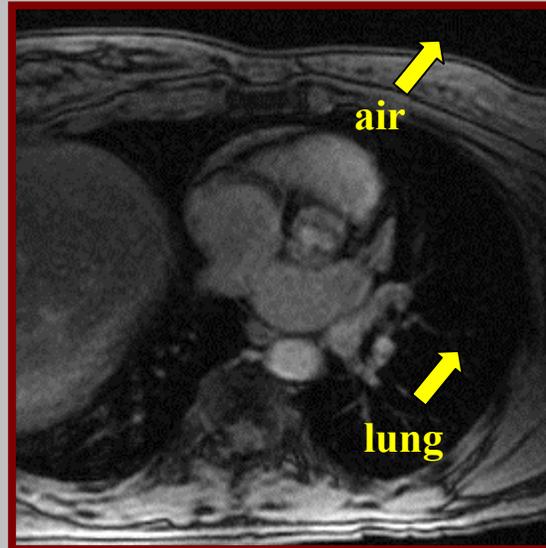
- **gradient echo** sequence

Phase contrast method

Noise

Additional remark: Air and lungs almost no signal in anatomical images.

➔ Phases purely accidental



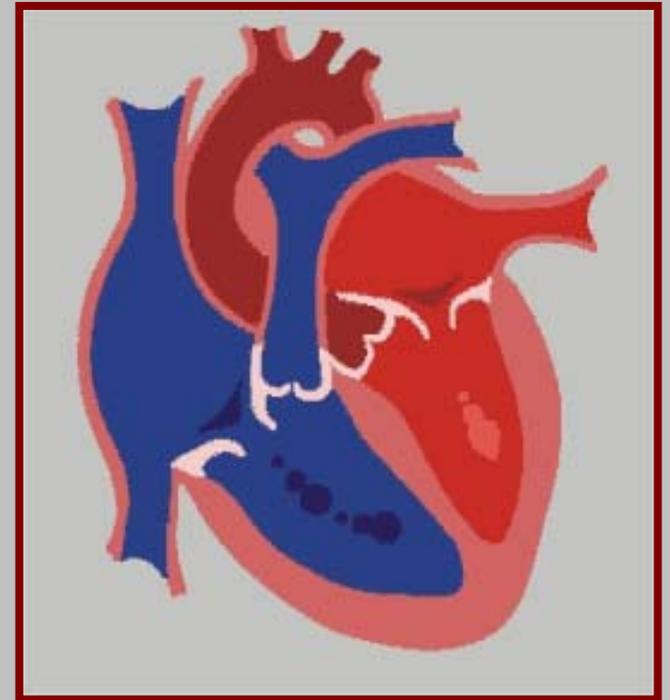
Pulsatility

ECG gating

Phase contrast technique concept as described up till now applies to **stationary** movement or flow.

But most rapid and important movement of cardiovascular system is rapidly **changing**.

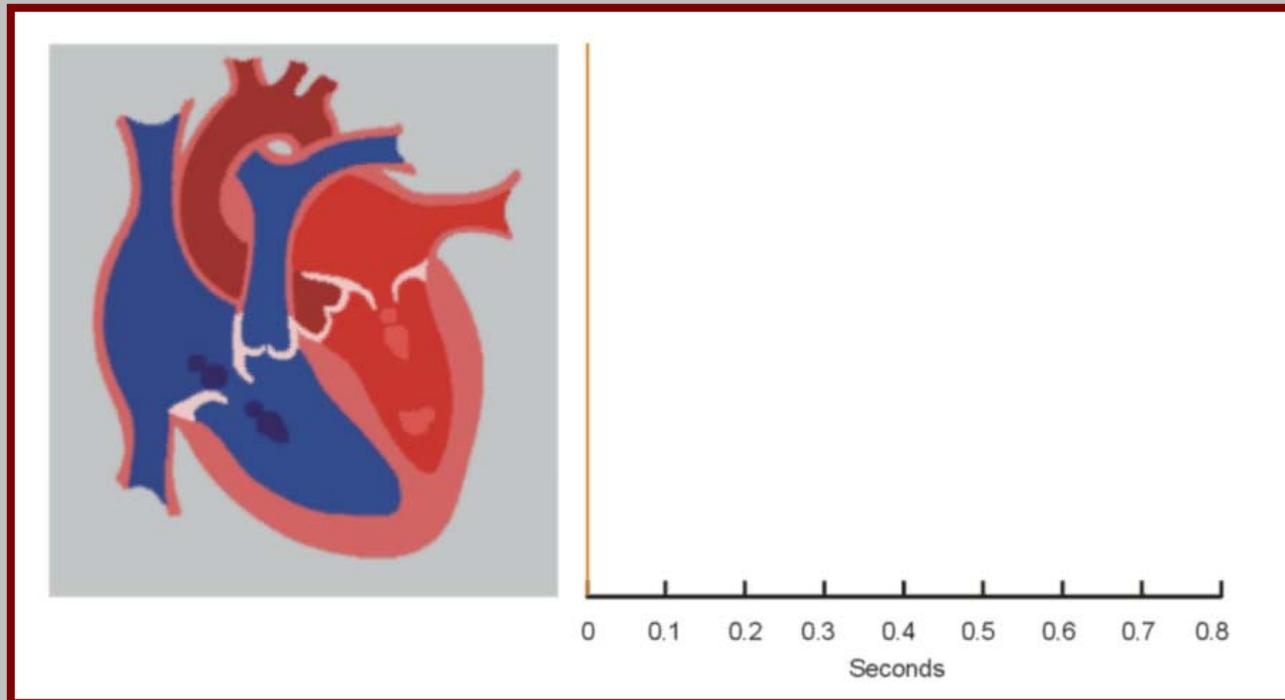
➔ Movement and flow (essentially) **periodic**.



Pulsatility

ECG gating

Periodic mechanical movement corresponds with periodical electrical activity (ECG).

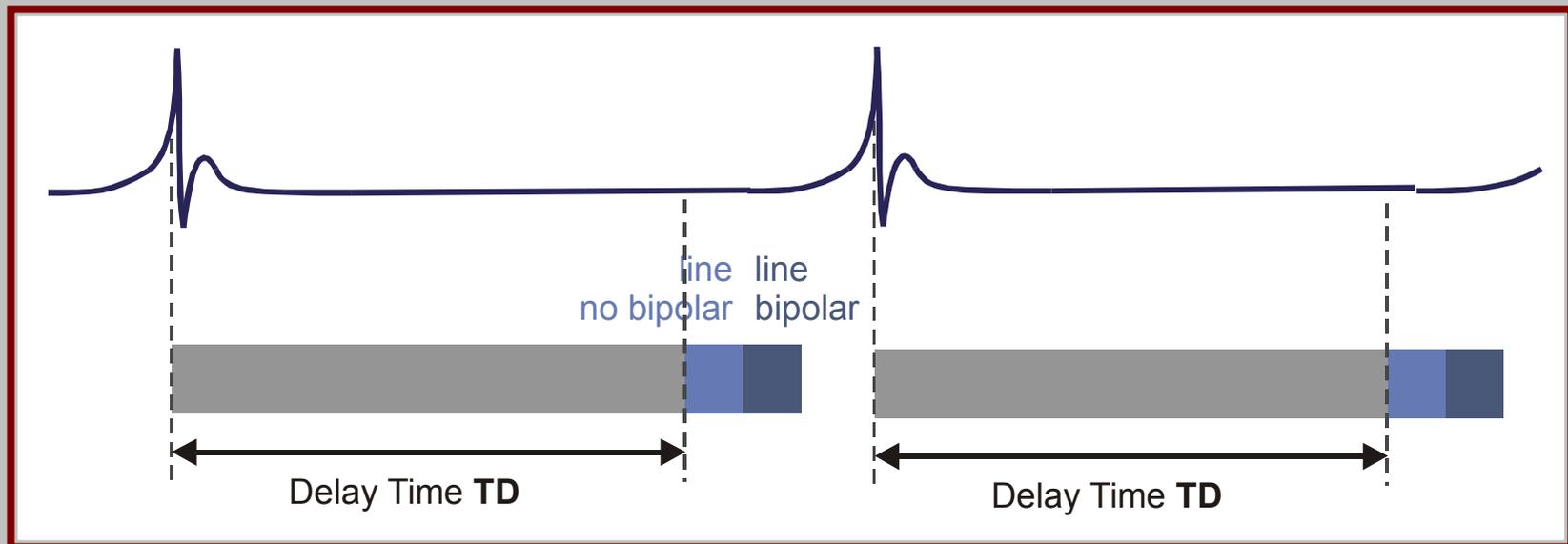


Pulsatility

ECG gating

Synchronization of data acquisition and electrical activity
= ECG gating

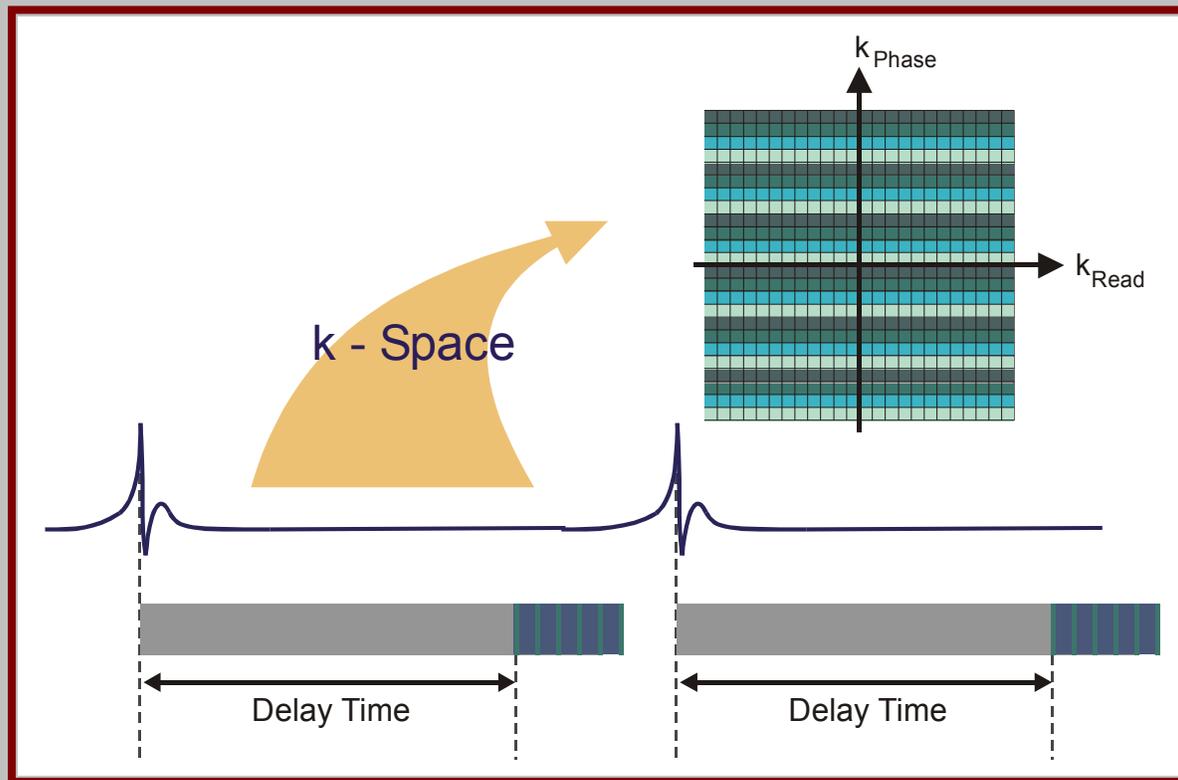
Typical **prospective**. Basically:



Pulsatility

ECG gating

Segmentation to improve speed:



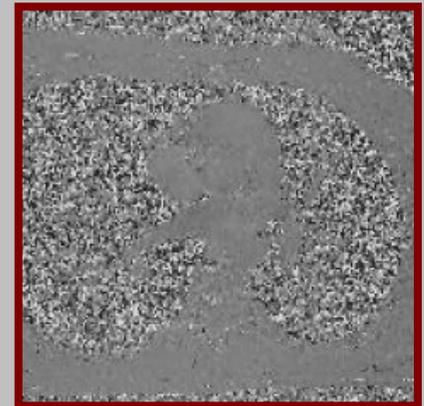
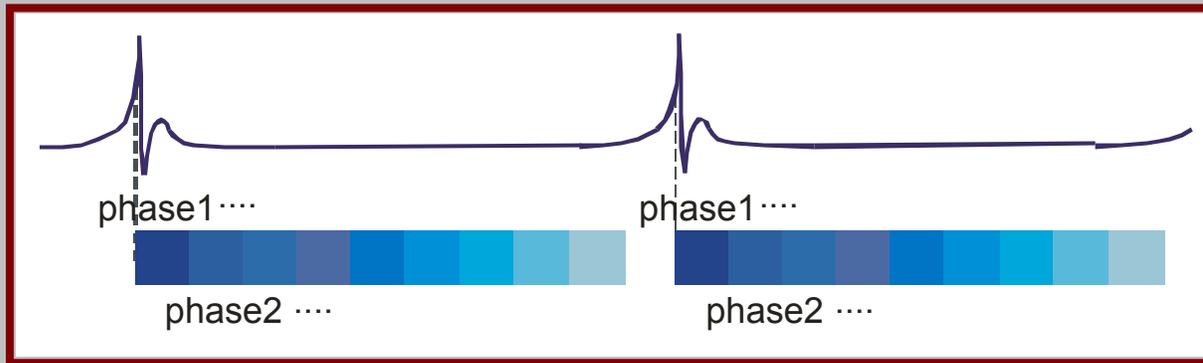
Longer time interval per heart beat, but outer data space lines do not contribute very much to „essential image information“.

Imaging time improvement here: 6 segments, consequently 4 instead of 24 heart beats.

Pulsatility

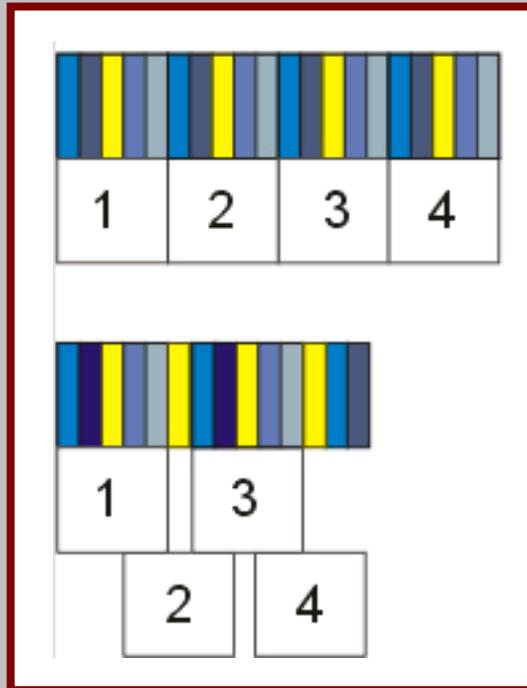
Cine Imaging

Images at different times in cardiac cycle within one sequence = **cine imaging**.



Pulsatility Cine Imaging

Echo sharing to
improve speed:



no echo sharing

echo sharing

➔ with segmentation and echo sharing phase contrast measurement within one breathhold.

Pulsatility

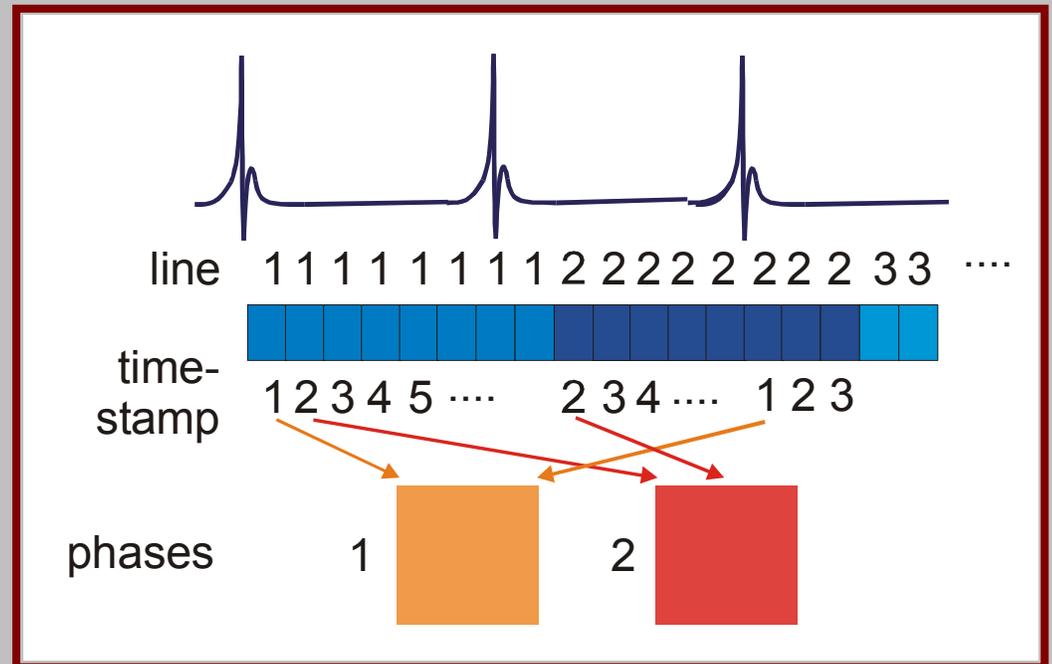
Cine Imaging

Heart frequency is not absolutely constant.

➔ 5-15% of data at the end of RR-interval missing

Alternative **retrospective ECG gating**. Basically:

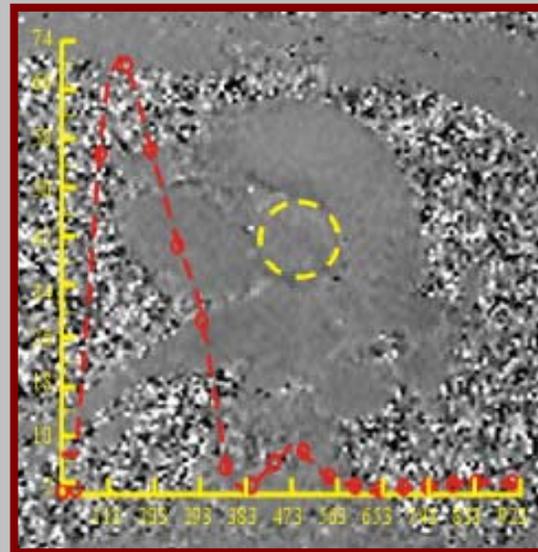
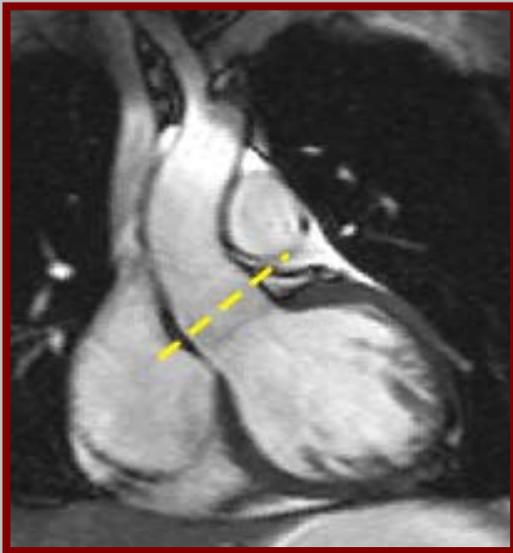
➔ Slower, but there are improvements.



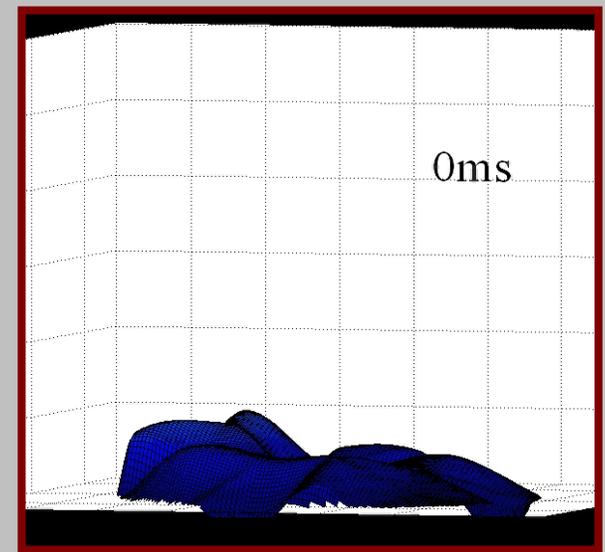
Archetypical postprocessing

Typical application: Cine through-plane phase contrast imaging of vessel cross-section.

➔ Region-of-interest = vessel cross-section



average velocity

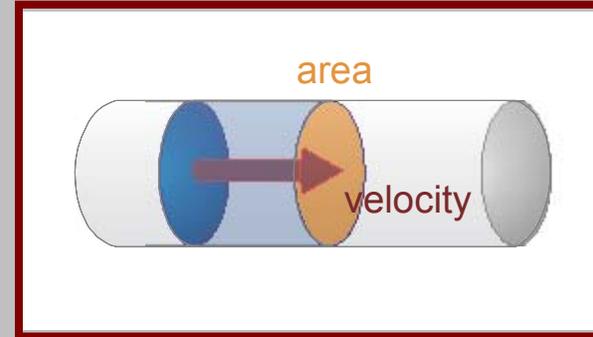


localized velocity

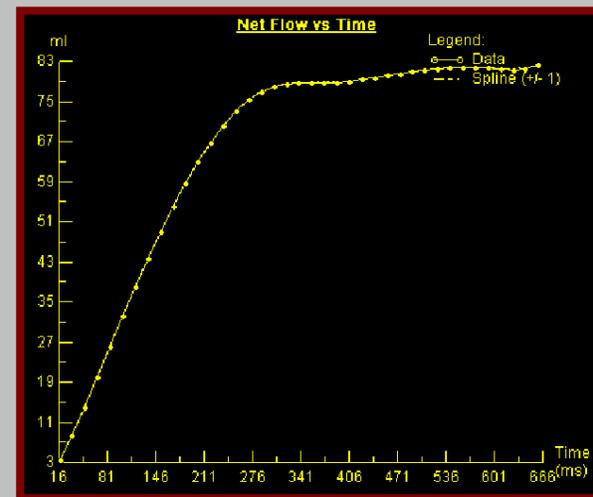
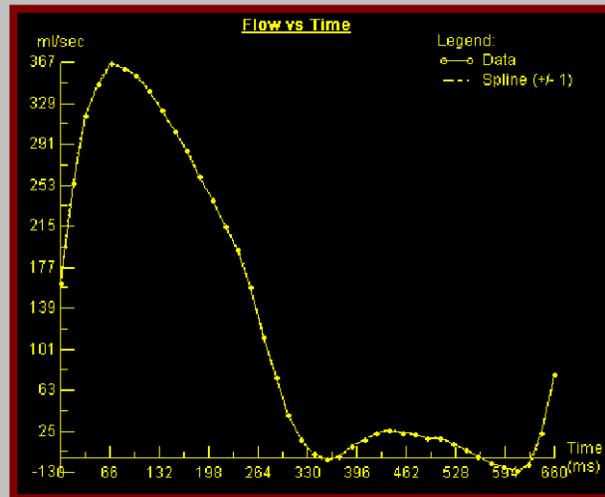
Archetypical postprocessing

Flow: $I = Av_{avg}$

$$\left(I = \frac{\Delta V}{\Delta t} = \frac{A\Delta s}{\Delta t} = Av_{avg} \right)$$



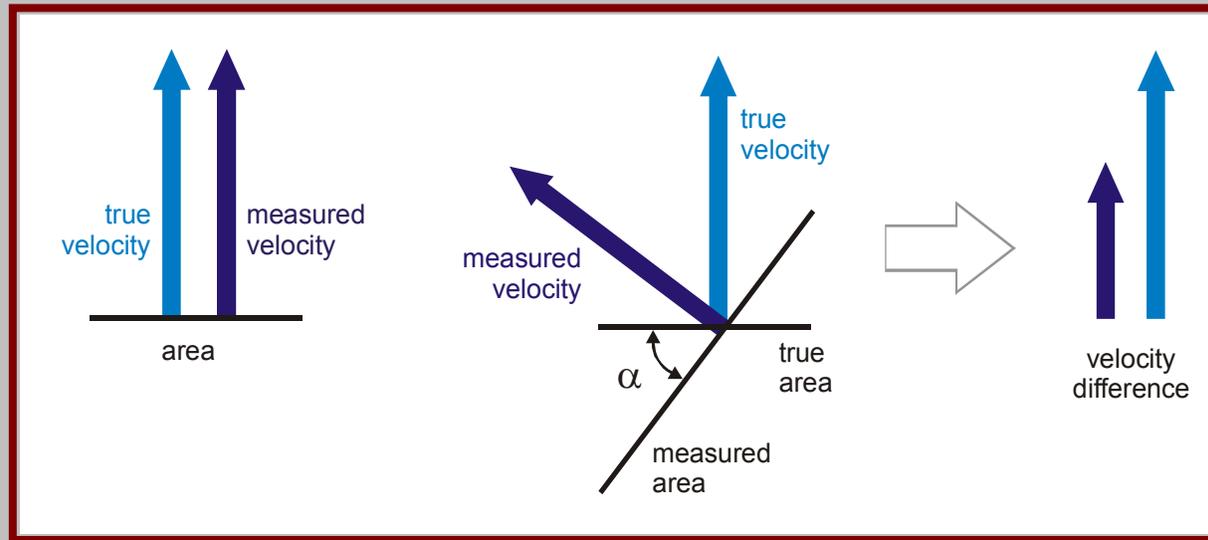
time resolved
flow



time integrated
flow = volume
passing per
cardiac cycle

Archetypical postprocessing

Remark: Correct placement of **imaging plane** different role for different quantities.

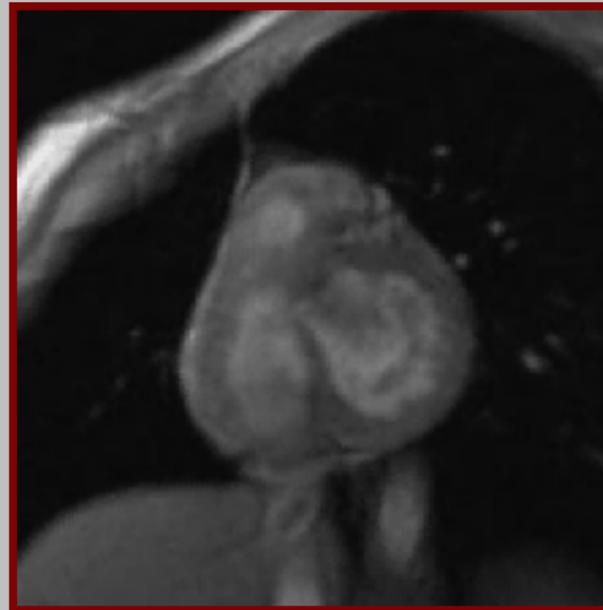
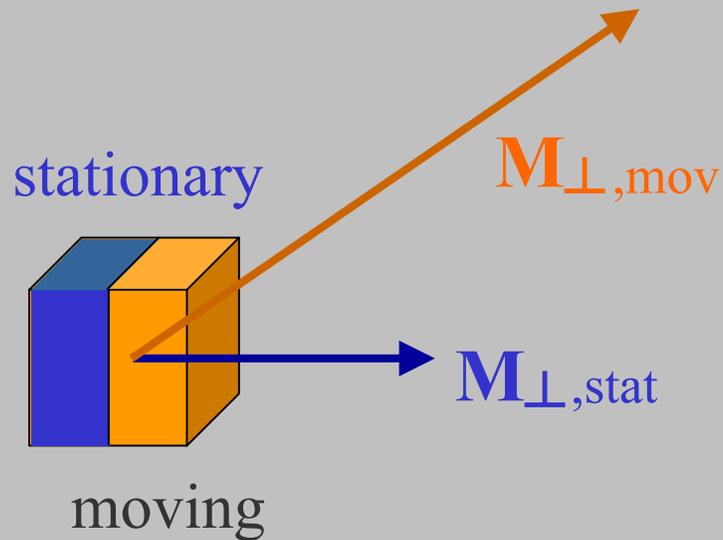


➔ Velocity: $v_{\text{meas}} = v_{\text{true}} \cos \alpha$
Flow: $I_{\text{meas}} = I_{\text{true}} \quad \left(A_{\text{meas}} = \frac{1}{\cos \alpha} A_{\text{true}} \right)$

Advanced Considerations

Partial volume effect

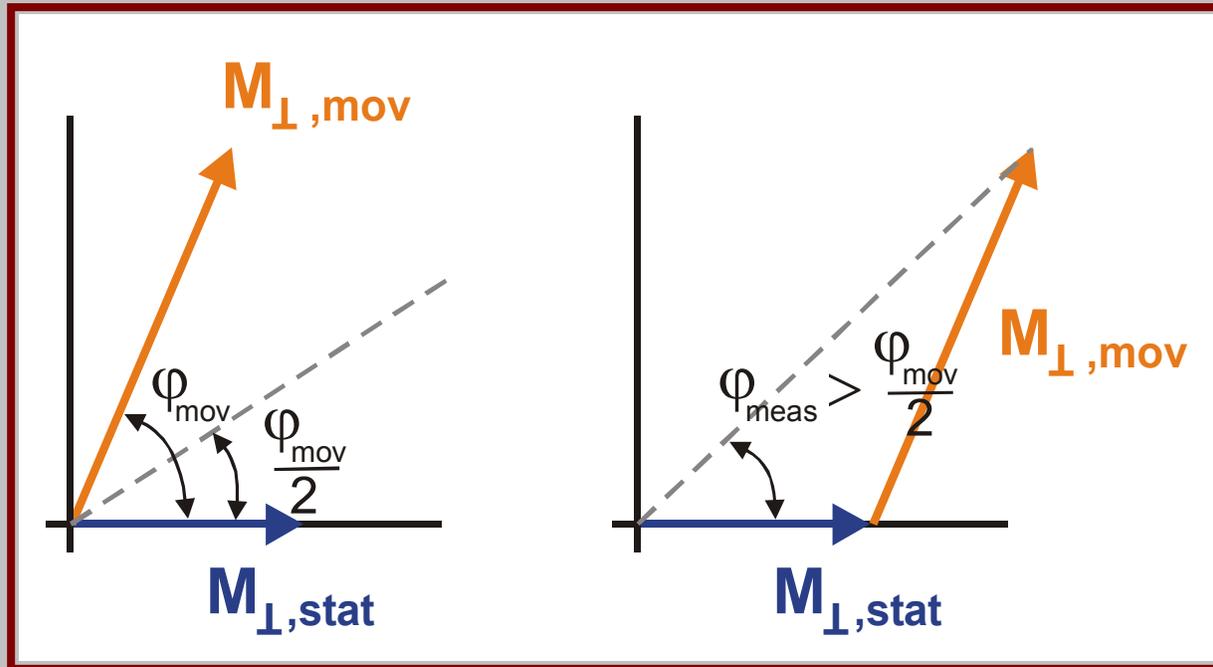
Partial volume effects **not linear** in phase measurements.



Tissue moving into plane has higher signal than stationary tissue.

Advanced Considerations

Partial volume effect

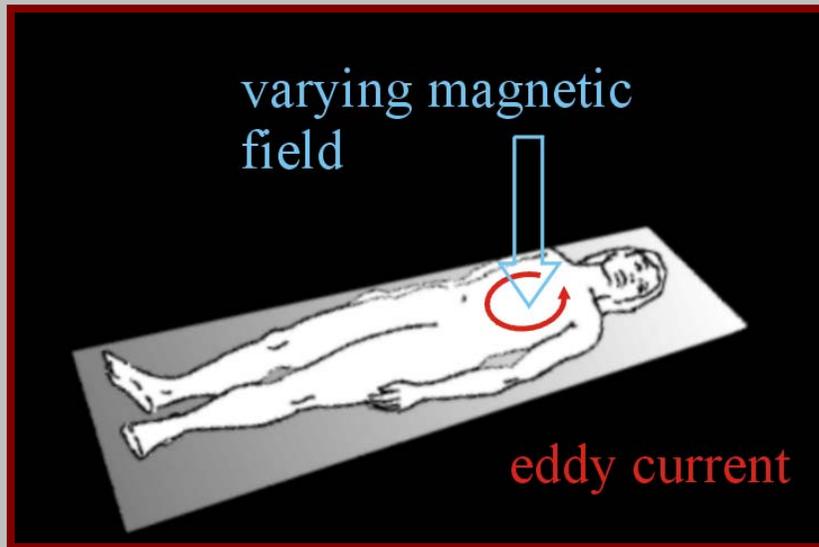


➔ Partial volume effect will typically lead to **overestimation** of flow.

Advanced Considerations

Eddy currents

Subtraction scheme introduced to suppress phase changes not caused by velocity. Bipolar gradients applied only for one data acquisition.



influences
phase(difference)



Base line correction =
subtraction of “velocity”
of stationary objects

Advanced Considerations

Maxwell correction

Gradient field must obey **Maxwell equations**.

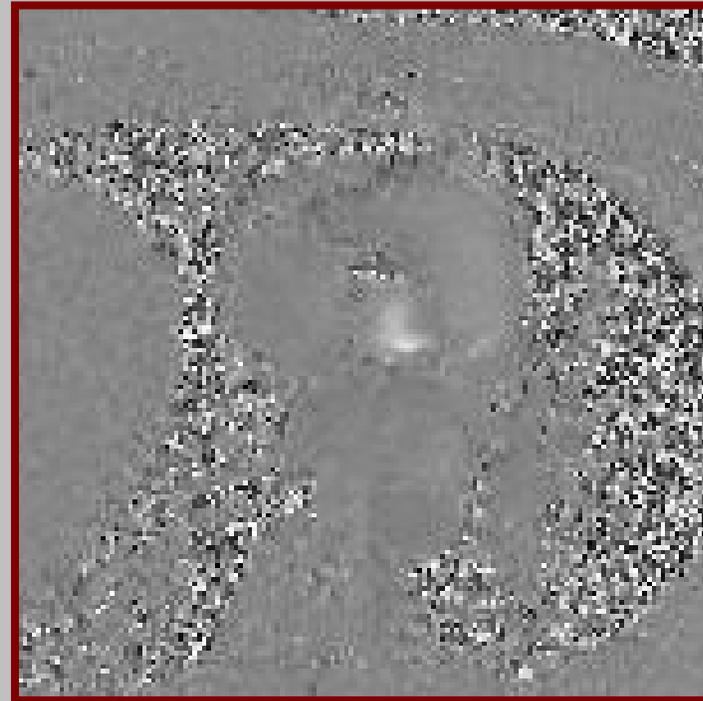
$$0 = \text{div } B_g(\mathbf{r}, t) \mathbf{e}_z = \text{div}(\mathbf{G}(t)\mathbf{r}) \mathbf{e}_z \quad \longrightarrow \quad G_z = 0$$

$$0 = \text{rot } B_g(\mathbf{r}, t) \mathbf{e}_z = \text{rot}(\mathbf{G}(t)\mathbf{r}) \mathbf{e}_z \quad \longrightarrow \quad G_x = G_y = 0$$

- ➔ Linear gradient field does **not exist**.
- ➔ Effect of **lowest order $O(\mathbf{r}^2)$** on phase differences, with \mathbf{r} distance to magnetic isocenter.
- ➔ Measurement **close to isocenter** or correction in image reconstruction.

Application examples

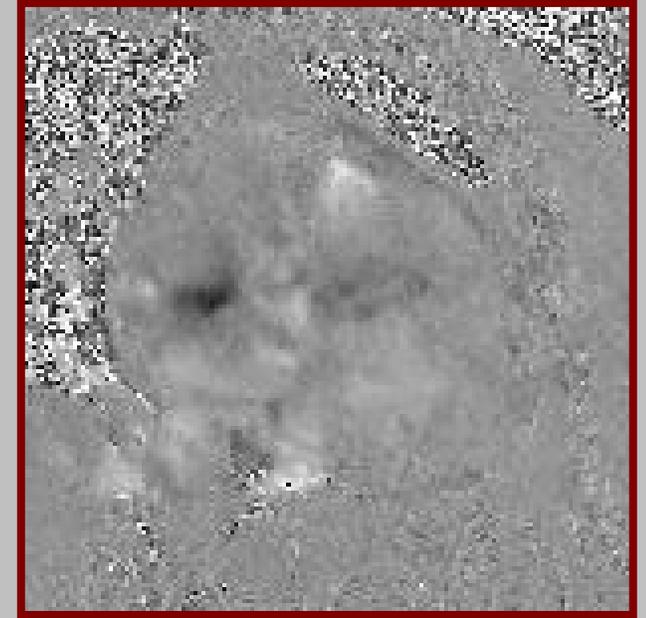
Application: Estimation of the degree of **stenoses**



$v_{\text{enc}} = 280 \text{ cm/s}$,
blood velocity up to 285 cm/s.

Application examples

Application: Verification of shunts

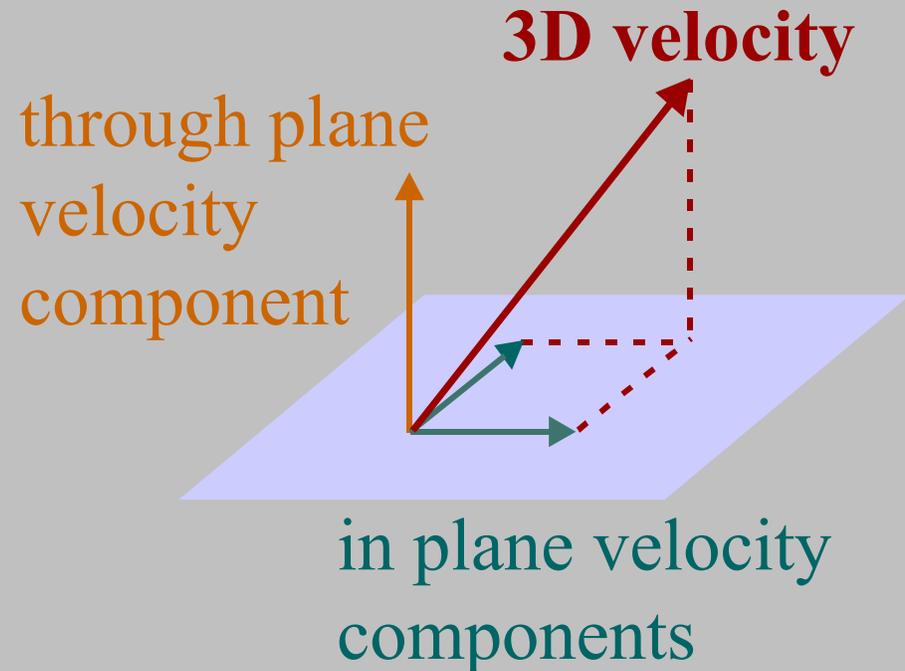
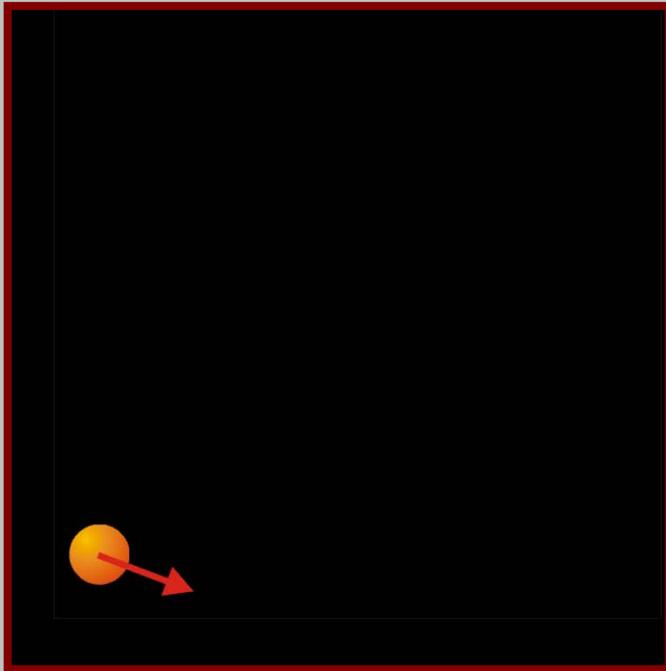


$v_{\text{enc}} = 100 \text{ cm/s}$,
blood velocity up to 105 cm/s.

Shunt volume = SV pulmonalis – SV aorta

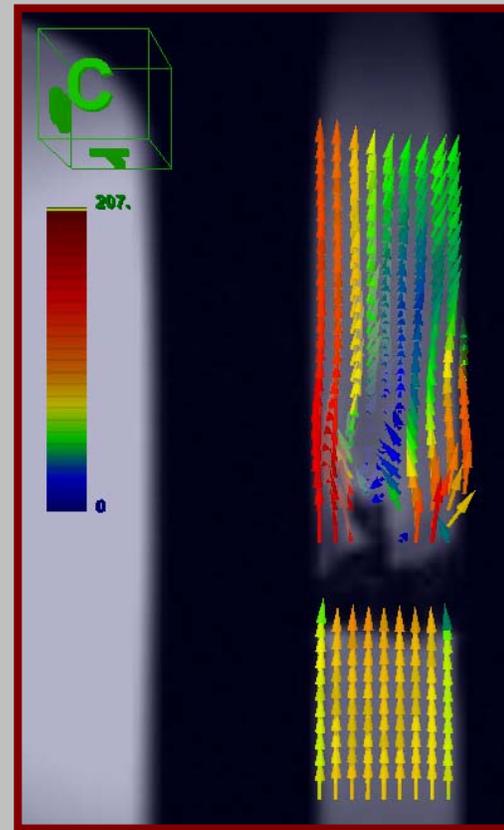
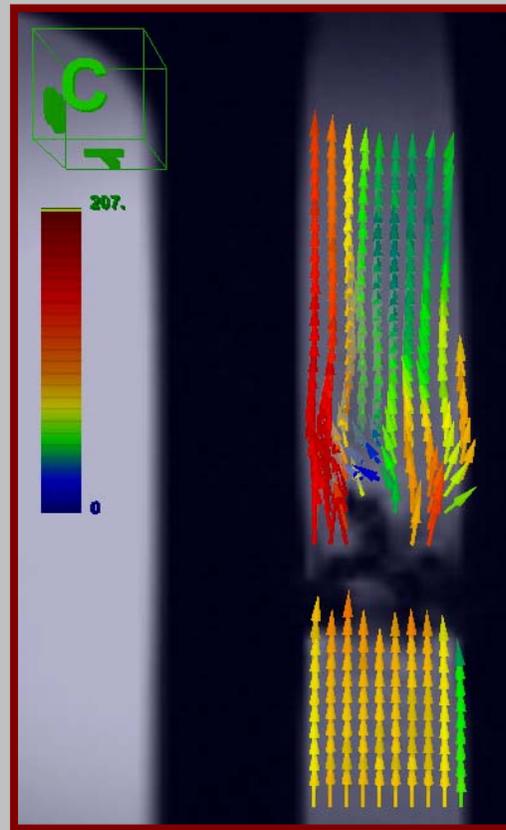
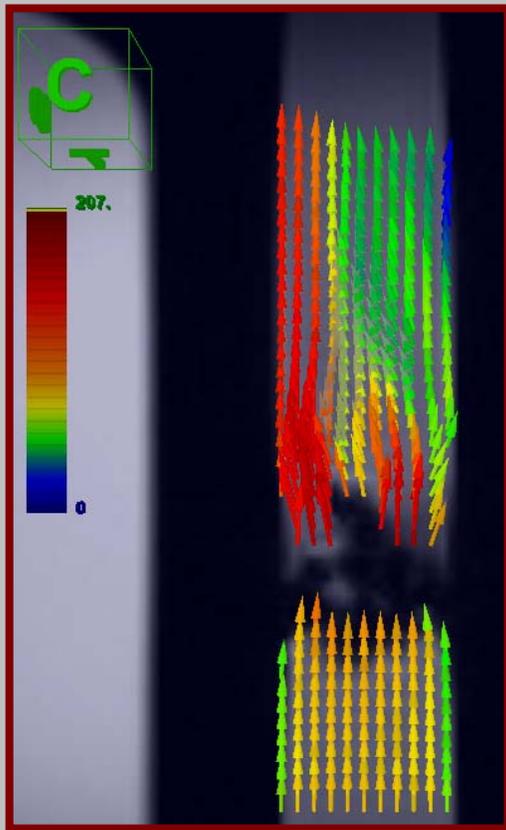
Perspectives

- Sequences (SNR, speed, parallel acquisition, navigator, ...)
- Segmentation ((semi)automatic contour detection)
- **3D or 4D velocity field**



Perspectives

➔ Flow patterns in **models**.

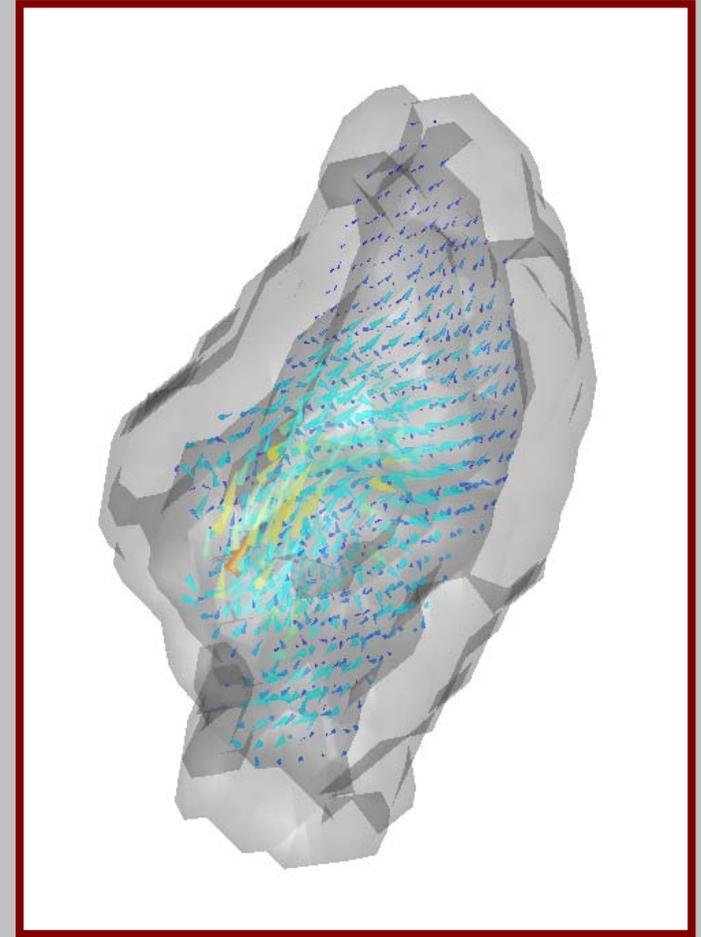
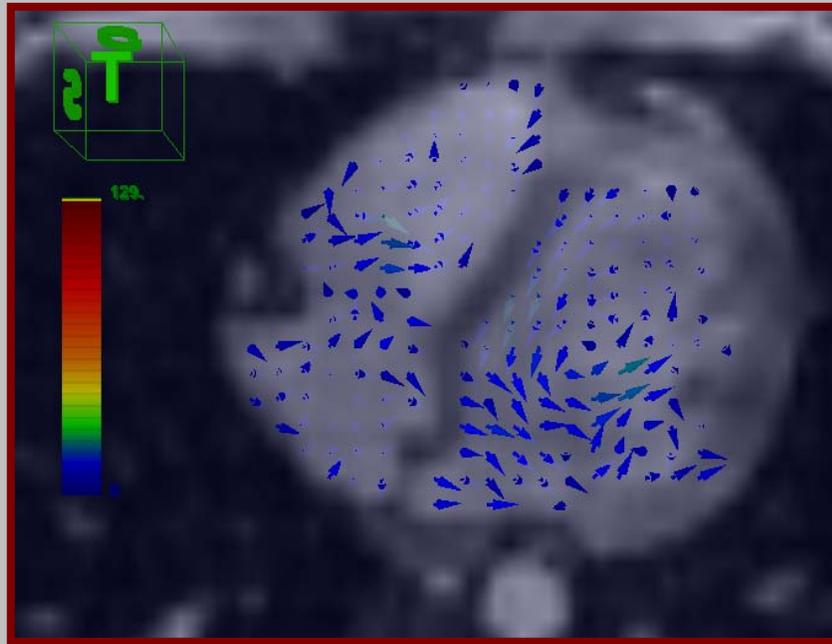


Stationary
water flow
through tube
with mechanical
valve.

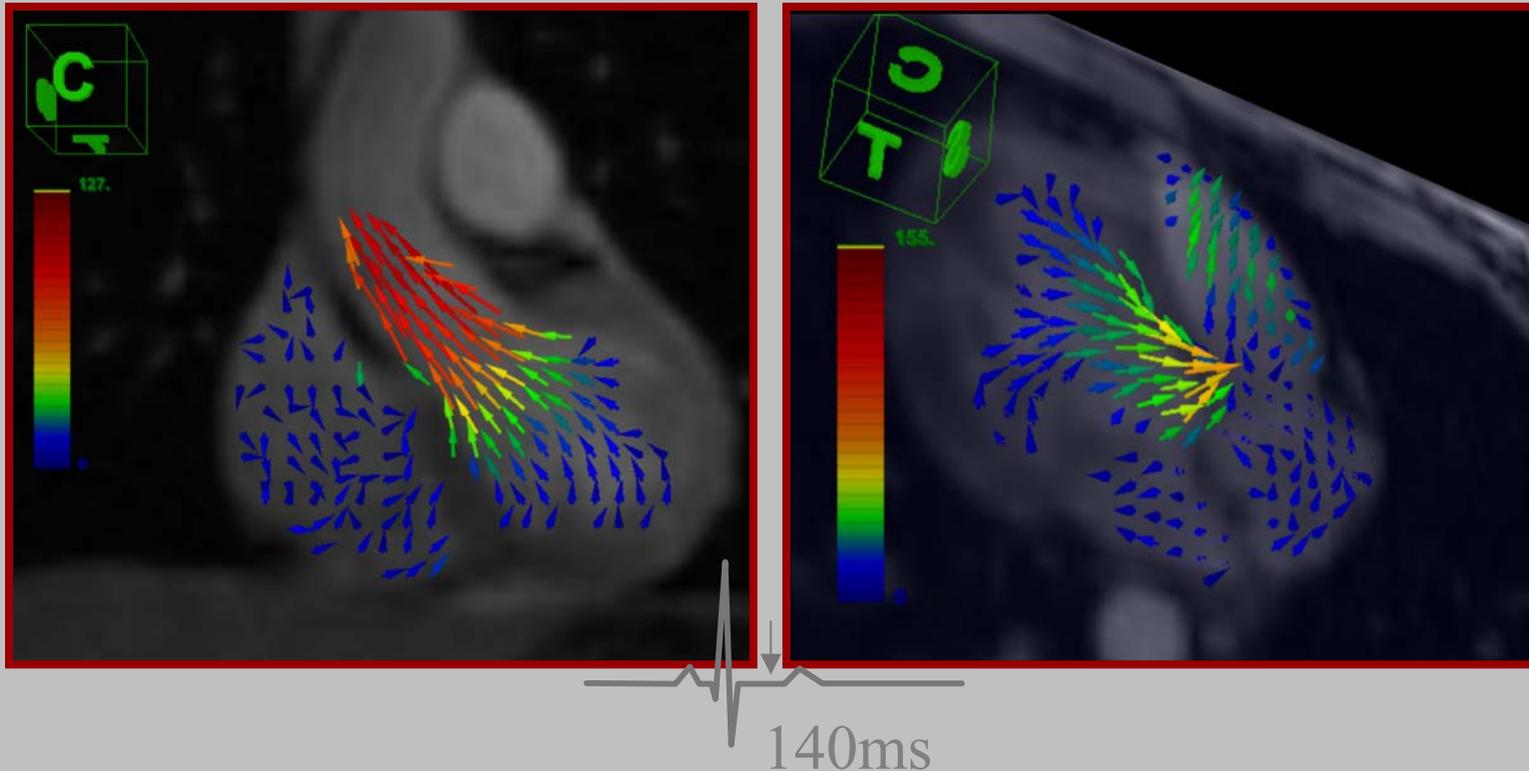
Perspectives

➔ Mechanical properties of
cardiovascular system.

Normal
blood flow
in the
heart.

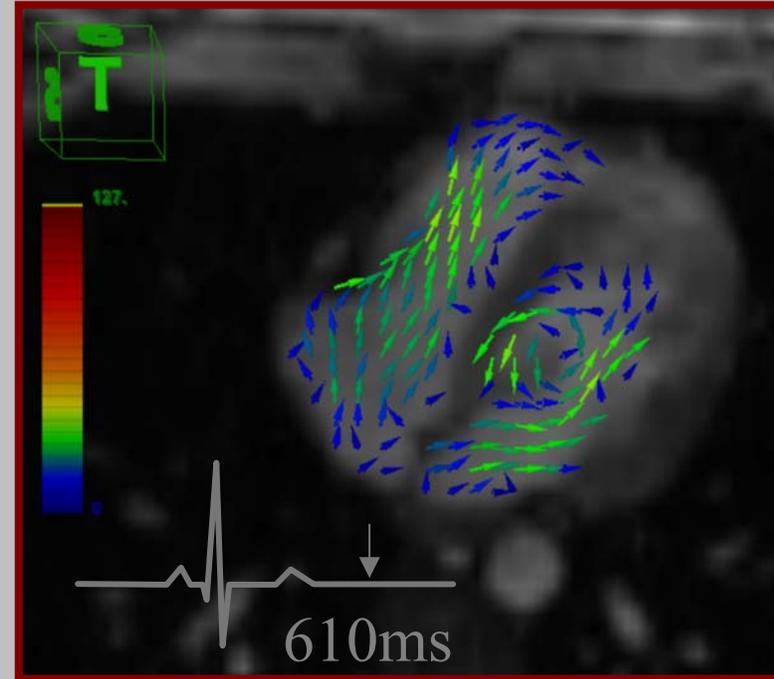
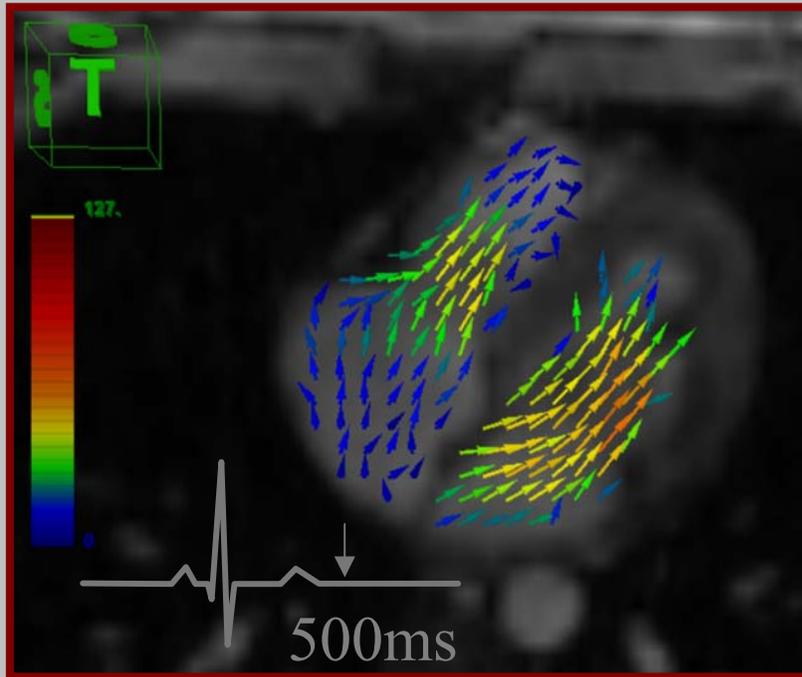


Perspectives



Normal left ventricular blood flow patterns in the **systole** – flow uniformly directed towards aorta.

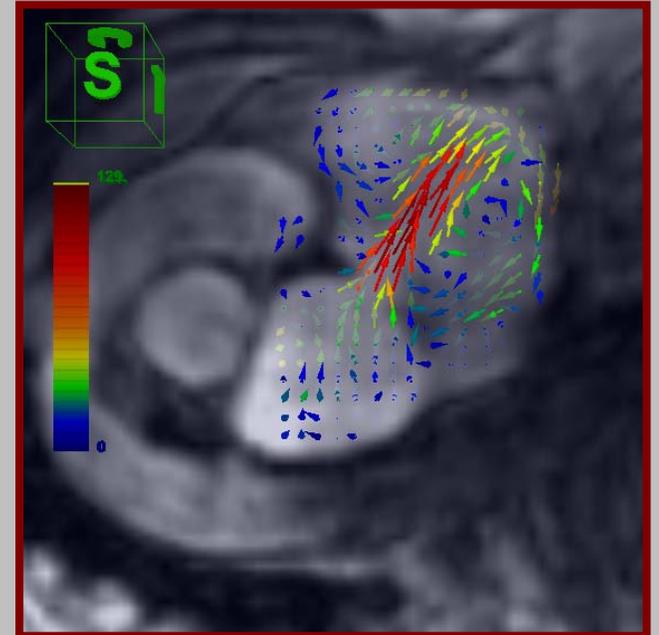
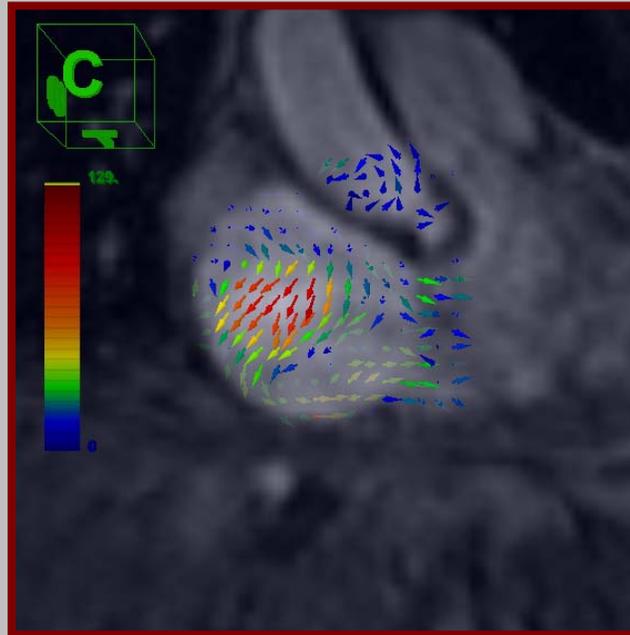
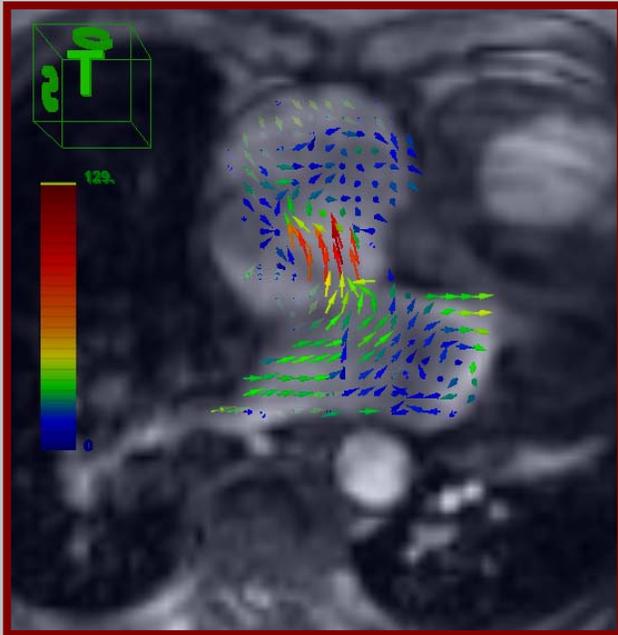
Perspectives



Normal left ventricular blood flow patterns in the **diastole** – first rather uniformly across whole orifice directed apically, then vortex formation.

Perspectives

➔ Detection and analysis of pathologies of cardiovascular system.



Blood flow through a shunt.