

### Shape representation to apply a transform in order to represent an object in terms of the transform coefficients, to describe the boundary that surrounds an object, to describe the region that is occupied by an object.

### Transform-based shape representation Fourier description wavelet-based analysis scale-space / multiscale characterization spherical harmonics – based description (3D)

### Contour-based shape representation • chain-code run-length polygonal approximation syntactic primitives spline snake / active contour multiscale primitives

Skeleton

praire-fire analogy: the boundary is set on fire

and skeleton is formed by the loci where the

fire fronts meet and quench each other;

the locus of the centers of all the maximal

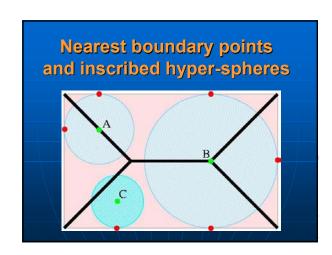
inscribed hyper-spheres.

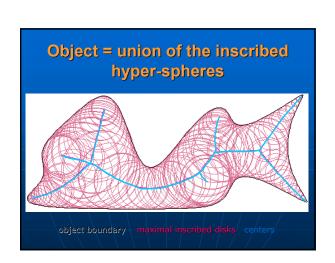
■ result of the Medial Axis Transform: object points having at least two closest boundary

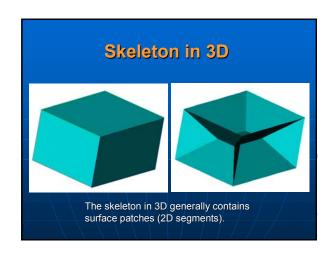
points;

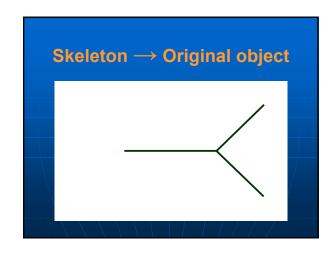
### Region-based shape representation polygon Voronoi / Delaunay quadtree morphological decomposition convex hull / deficiency ■ run-length distance transform

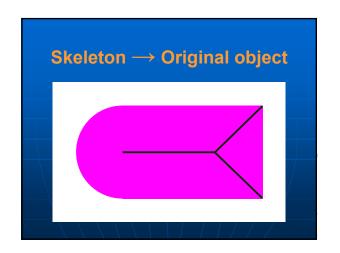
## ■ \....

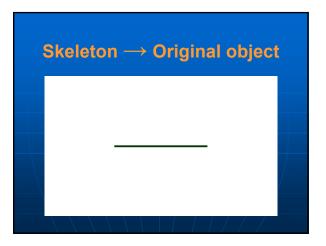


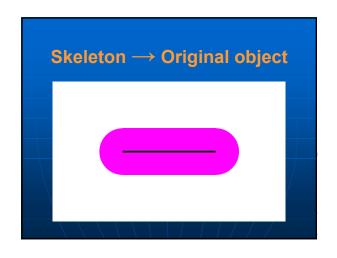


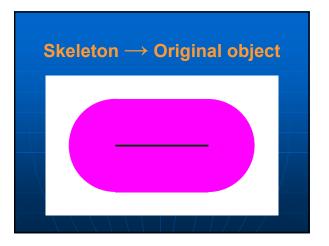


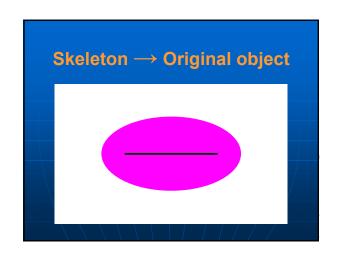


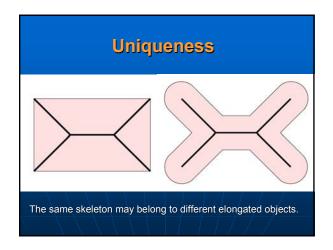


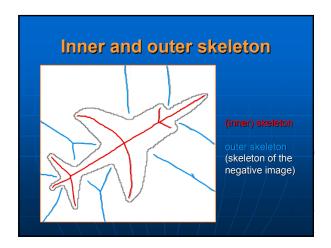


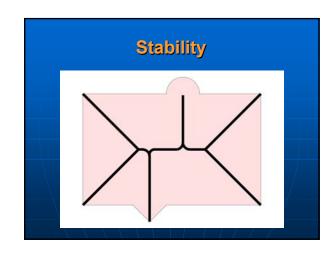


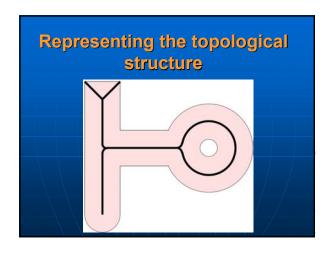




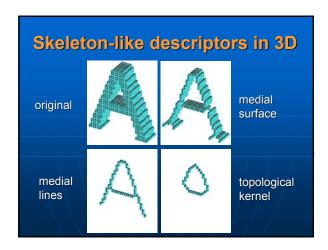


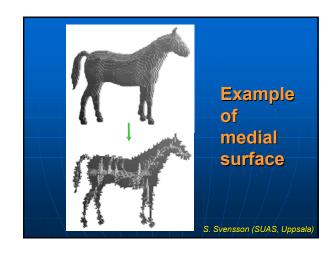


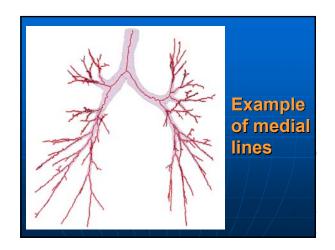


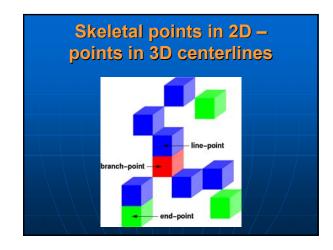


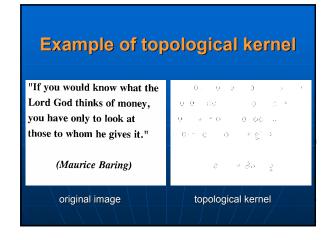
# Properties • represents • the general form of an object, • the topological structure of an object, and • local object symmetries. • invariant to • translation, • rotation, and • (uniform) scale change. • simplified and thin.

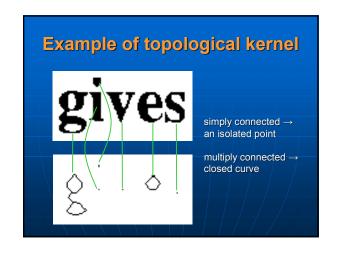






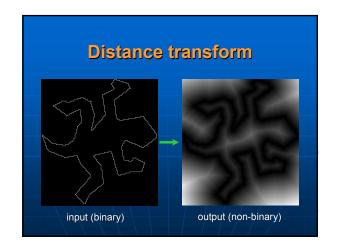


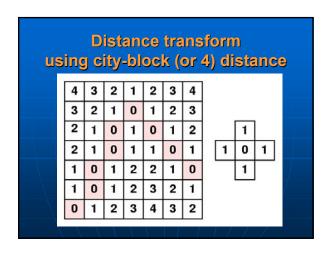


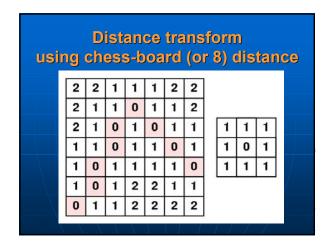




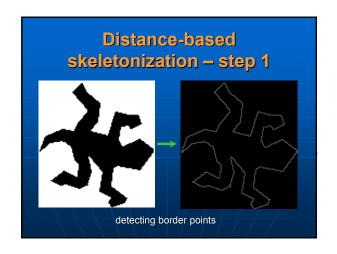
### Input: Binary array A containing feature elements (1's) and non-feature elements (0's). Output: Non-binary array B containing the distance to the closest feature element.

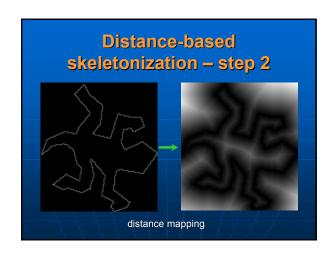


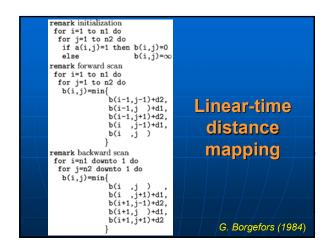


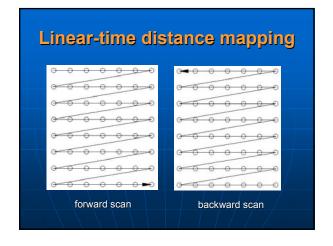


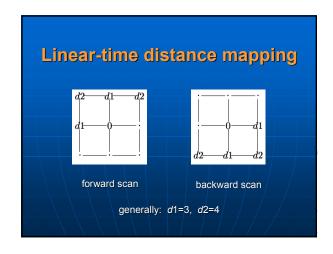
### Distance-based skeletonization 1. Border points (as feature elements) are extracted from the original binary image. 2. Distance transform is executed (i.e., distance map is generated). 3. The ridges (local extremas) are detected as skeletal points.



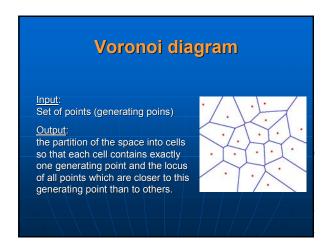


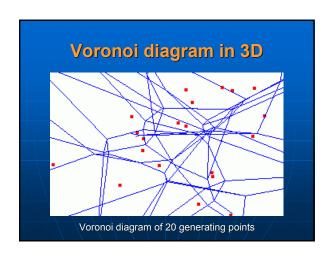


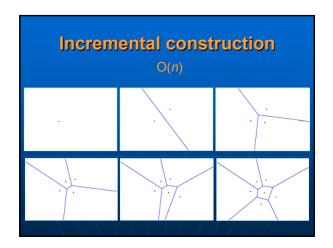


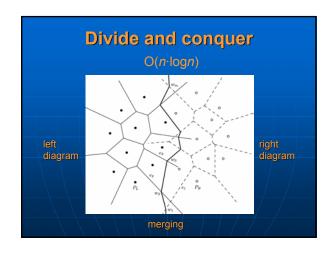


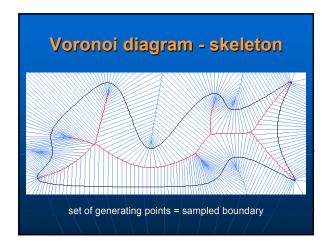


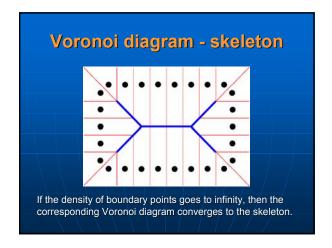


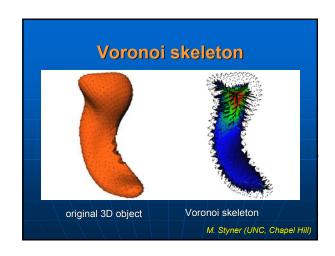


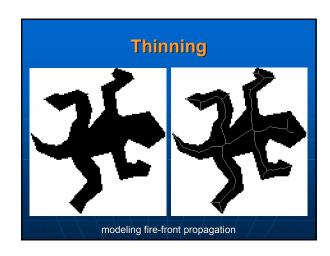


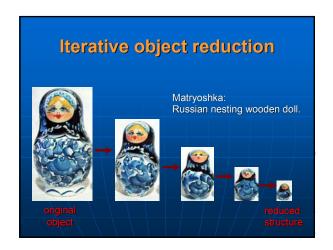




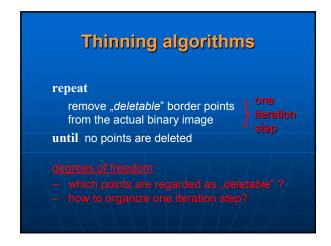


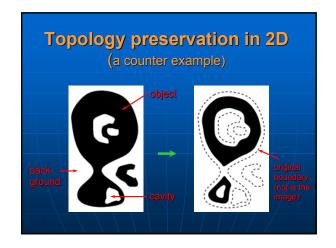


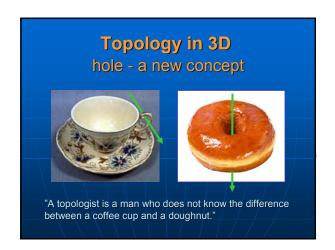


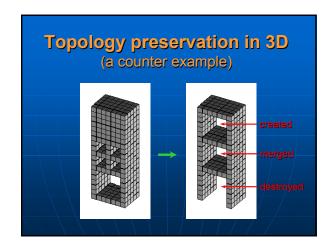












### **Shape preservation**

"If you would know what the Lord God thinks of money, you have only to look at those to whom he gives it."

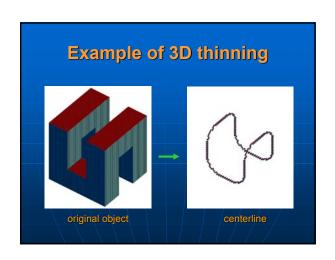
(Maurice Baring)

### Shape preservation

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## Example of 2D thining william Stark fatake



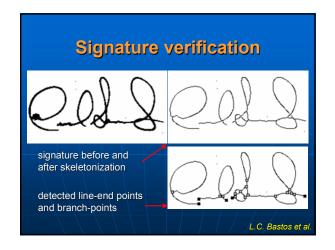
### allows direct centerline extraction in 3D, makes easy implementation possible, takes the least computational costs, and can be executed in parallel.

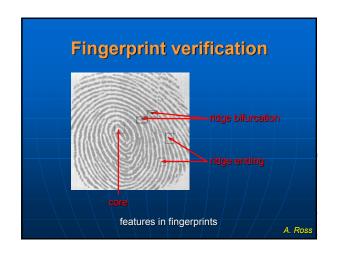
### Requirements - Geometrical: The skeleton must be in the middle of the original object and must be invariant to translation, rotation, and scale change. - Topological: The skeleton must retain the topology of the original object.

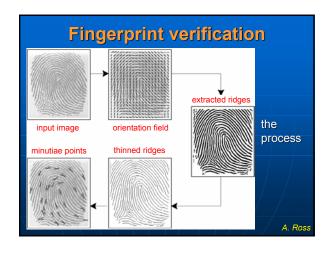
	C	Comparison thod geometrical topological		
	method	geometrical	topological	
	distance-based	yes	no	
	Voronoi-based	yes	yes	
\	thinning	no	yes	

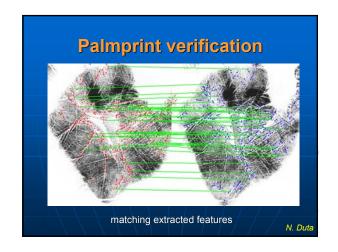


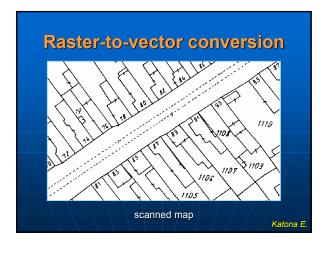


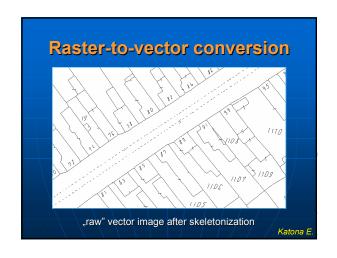


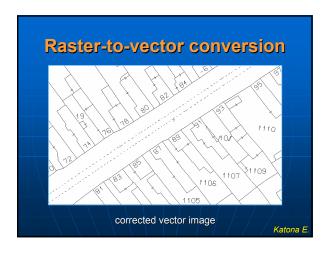


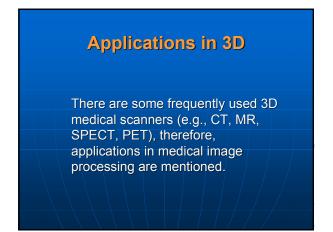


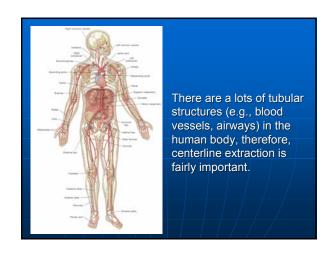


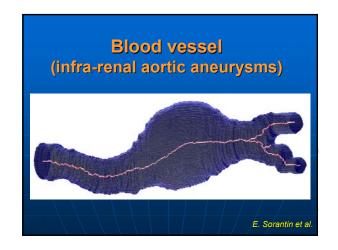




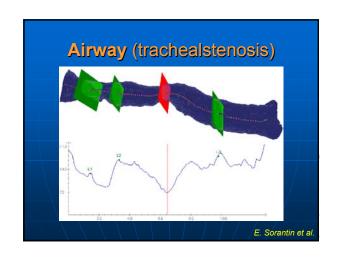


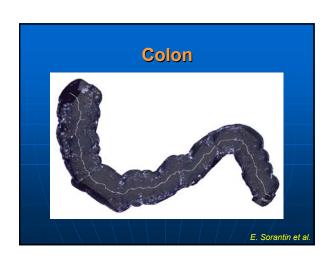


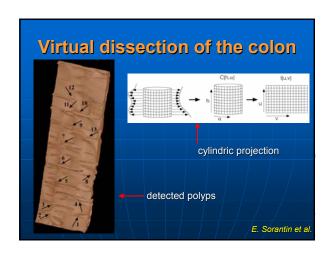


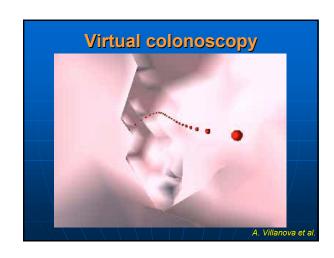


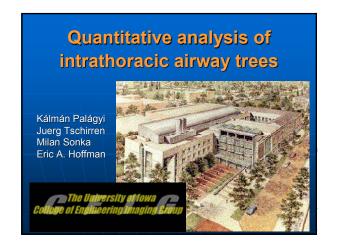


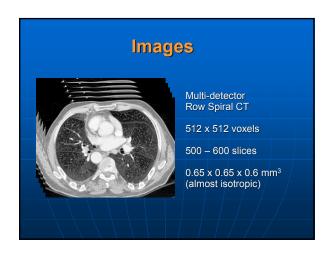


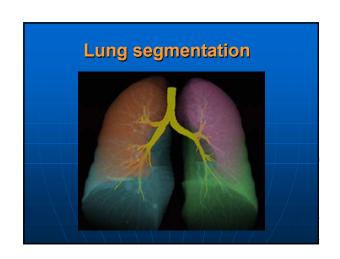


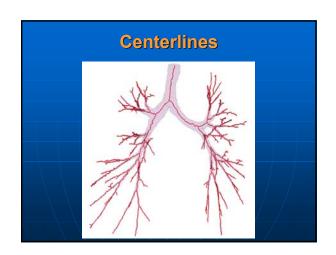


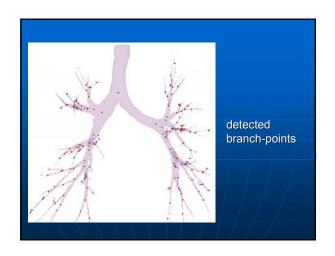


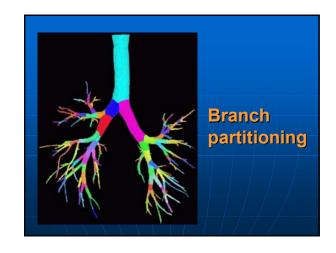


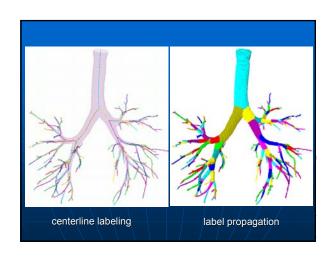


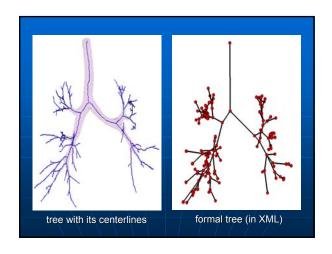












### Quantitative indices for tree branches

- <u>length</u> (Euclidean distance between the parent and the child branch points)
- volume (volume of all voxels belonging to the branch)
- <u>surface area</u> (surface area of all boundary voxels belonging to the branch)
- <u>average diameter</u> (assuming cylindric segments)

