

# Multi-modal Human-computer Interaction

Attila Fazekas

Attila.Fazekas@inf.unideb.hu

SSIP 2008, 9 July 2008



# Hungary and Debrecen

9 July, 2008  
SSIP'09





# Debrecen – Big Church

9 July, 2008  
SSIP '09





# University of Debrecen

9 July, 2008  
SSIP'09





# Coming Soon

9 July, 2008  
SSIP '09

➔ Summer School on Image Processing 2009



# Coming Soon

9 July, 2008  
SSIP'09

➔ Summer School on Image Processing 2009

➔  **SSIP 2009**  
17th Summer School on Image Processing  
6 July - 15 July, Debrecen, Hungary



# Coming Soon

9 July, 2008  
SSIP'09

➔ Summer School on Image Processing 2009



**SSIP 2009**  
17th Summer School on Image Processing  
6 July - 15 July, Debrecen, Hungary

➔ <http://www.inf.unideb.hu/~SSIP>



# Road Map

9 July, 2008  
SSIP'09

- ➔ Multi-modal interactions and systems (main categories, examples, benefits)
- ➔ Turk-2 – Multi-modal chess player
- ➔ Face detection, facial gestures recognition
- ➔ Experimental results
- ➔ Examples





# Defining Multi-Modal Interaction

9 July, 2008  
SSIP '09

➔ There are two views on multi-modal interaction:

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Defining Multi-Modal Interaction

9 July, 2008  
SSIP '09

- ➔ There are two views on multi-modal interaction:
  - ➔➔ The first focuses on the human side: perception and control. There the word modality refers to human input and output channels.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Defining Multi-Modal Interaction

9 July,2008  
SSIP'09

- ➔ There are two views on multi-modal interaction:
  - The first focuses on the human side: perception and control. There the word modality refers to human input and output channels.
  - The second view focuses on synergistic using two or more computer input or output modalities.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Human-Centered View

9 July, 2008  
SSIP '09

➔ The focus is on multi-modal perception and control, that is, human input and output channels.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Human-Centered View

9 July, 2008  
SSIP '09

- ➔ The focus is on multi-modal perception and control, that is, human input and output channels.
- ➔ Perception means the process of transforming sensory information to higher-level representation.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# The Modalities

9 July, 2008  
SSIP '09

➔ We can divide the modalities in seven groups

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# The Modalities

9 July,2008  
SSIP'09

- ➔ We can divide the modalities in seven groups
  - ▮➔ Internal chemical (blood oxygen, etc.)

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# The Modalities

9 July, 2008  
SSIP '09

- ➔ We can divide the modalities in seven groups
  - ▣➔ Internal chemical (blood oxygen, etc.)
  - ▣➔ External chemical (taste, etc.)

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM





# The Modalities

9 July, 2008  
SSIP '09

- ➔ We can divide the modalities in seven groups
  - ▣➔ Internal chemical (blood oxygen, etc.)
  - ▣➔ External chemical (taste, etc.)
  - ▣➔ Somatic senses (touch, etc.)

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# The Modalities

9 July, 2008  
SSIP '09

- ➔ We can divide the modalities in seven groups
  - ▣➔ Internal chemical (blood oxygen, etc.)
  - ▣➔ External chemical (taste, etc.)
  - ▣➔ Somatic senses (touch, etc.)
  - ▣➔ Muscle sense (stretch, etc.)

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# The Modalities

9 July, 2008  
SSIP'09

- ➔ We can divide the modalities in seven groups
  - ▣➔ Internal chemical (blood oxygen, etc.)
  - ▣➔ External chemical (taste, etc.)
  - ▣➔ Somatic senses (touch, etc.)
  - ▣➔ Muscle sense (stretch, etc.)
  - ▣➔ Sense of balance

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# The Modalities

9 July,2008  
SSIP'09

- ➔ We can divide the modalities in seven groups
  - ▣➔ Internal chemical (blood oxygen, etc.)
  - ▣➔ External chemical (taste, etc.)
  - ▣➔ Somatic senses (touch, etc.)
  - ▣➔ Muscle sense (stretch, etc.)
  - ▣➔ Sense of balance
  - ▣➔ **Hearing**

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# The Modalities

9 July, 2008  
SSIP'09

➔ We can divide the modalities in seven groups

➤ Internal chemical (blood oxygen, etc.)

➤ External chemical (taste, etc.)

➤ Somatic senses (touch, etc.)

➤ Muscle sense (stretch, etc.)

➤ Sense of balance

➤ **Hearing**

➤ **Vision**

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# System-Centered View

9 July, 2008  
SSIP '09

➔ In computer science multi-modal user interfaces have been defined in many ways.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# System-Centered View

9 July,2008  
SSIP'09

- ➔ In computer science multi-modal user interfaces have been defined in many ways.
- ➔ Chatty's explanation of multi-modal interaction is the one that most computer scientist use. With the term **multi-modal user interface** they mean a system that accepts many different inputs that are combined in a meaningful way.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Definition of the Multimodality

9 July,2008  
SSIP'09

➔ "Multi-modality is the capacity of the system to communicate with a user along different types of communication channels."

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM





# Definition of the Multimodality

9 July,2008  
SSIP'09

- ➔ "Multi-modality is the capacity of the system to communicate with a user along different types of communication channels."
- ➔ Both multimedia and multi-modal systems use multiple communication channels.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Definition of the Multimodality

9 July,2008  
SSIP'09

- ➔ "Multi-modality is the capacity of the system to communicate with a user along different types of communication channels."
- ➔ Both multimedia and multi-modal systems use multiple communication channels. **But a multi-modal system strives for meaning.**

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Two Types of Multi-modal Systems

9 July, 2008  
SSIP '09

➔ The goal is to use the computer as a tool.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Two Types of Multi-modal Systems

9 July,2008  
SSIP'09

- ➔ The goal is to use the computer as a tool.
- ➔ The computer as a dialogue partner.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# History

9 July, 2008  
SSIP '09

➔ Bolt's Put-That-There system

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# History

9 July,2008  
SSIP'09

➔ Bolt's Put-That-There system. In this system the user could move objects on screen by pointing and speaking.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# History

9 July,2008  
SSIP'09

- ➔ Bolt's Put-That-There system. In this system the user could move objects on screen by pointing and speaking.
- ➔ CUBRICON is a system that uses mouse pointing and speech.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# History

9 July,2008  
SSIP'09

- ➔ Bolt's Put-That-There system. In this system the user could move objects on screen by pointing and speaking.
- ➔ CUBRICON is a system that uses mouse pointing and speech.
- ➔ Oviatt presented a multi-modal system for dynamic interactive maps.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM





# Benefits

9 July, 2008  
SSIP '09

➔ **Efficiency** follows from using each modality for the task that it is best suited for.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Benefits

9 July, 2008  
SSIP '09

- ➔ **Efficiency** follows from using each modality for the task that it is best suited for.
- ➔ **Redundancy** increases the likelihood that communication proceeds smoothly because there are many simultaneous references to the same issue.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Benefits

9 July, 2008  
SSIP '09

- ➔ **Efficiency** follows from using each modality for the task that it is best suited for.
- ➔ **Redundancy** increases the likelihood that communication proceeds smoothly because there are many simultaneous references to the same issue.
- ➔ **Perceptability** increases when the tasks are facilitated in spatial context.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Benefits

9 July,2008  
SSIP'09

➔ **Naturalness** follows from the free choice of modalities and may result in a human-computer communication that is close to human-human communication.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Benefits

9 July,2008  
SSIP'09

- ➔ **Naturalness** follows from the free choice of modalities and may result in a human-computer communication that is close to human-human communication.
- ➔ **Accuracy** increases when another modality can indicate an object more accurately than the main modality.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Benefits

9 July,2008  
SSIP'09

➔ **Synergy** occurs when one channel of communication can help refine imprecision, modify the meaning, or resolve ambiguities in another channel.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Applications

9 July, 2008  
SSIP '09

➔ Mobile telecommunication

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Applications

9 July, 2008  
SSIP '09

- ➔ Mobile telecommunication
- ➔ Hands-free devices to computers

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM





# Applications

9 July, 2008  
SSIP '09

- ➔ Mobile telecommunication
- ➔ Hands-free devices to computers
- ➔ Using in a car

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Applications

9 July, 2008  
SSIP '09

- ➔ Mobile telecommunication
- ➔ Hands-free devices to computers
- ➔ Using in a car
- ➔ Interactive information panel

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Turk-2

9 July, 2008  
SSIP'09



MMHCI

Turk 2

Face detection

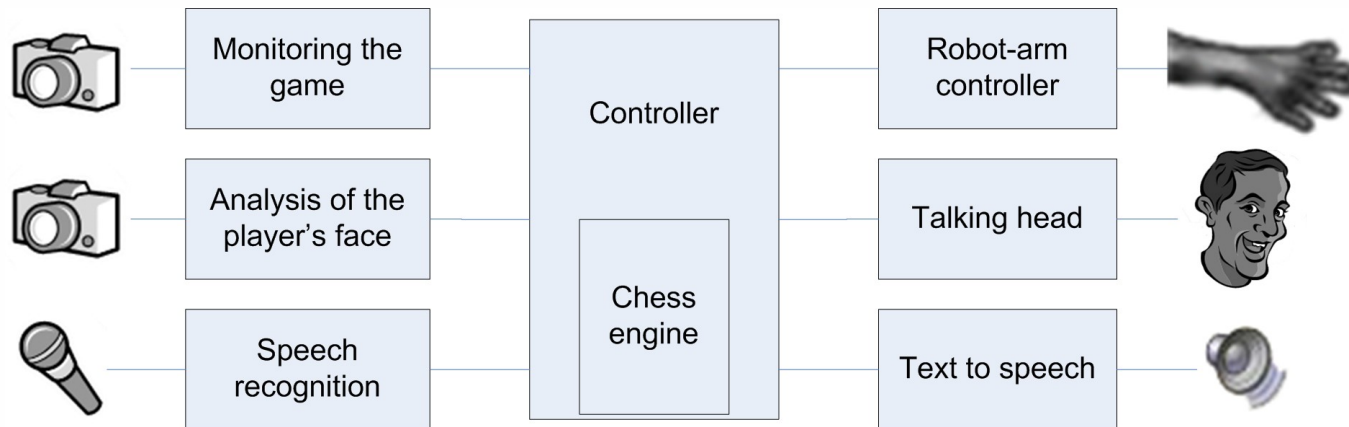
Face gesture

Examples

SVM

# System Components

9 July, 2008  
SSIP '09



MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Introduction

9 July, 2008  
SSIP'09

➔ Faces are our interfaces in our emotional and social life.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Introduction

9 July, 2008  
SSIP '09

- ➔ Faces are our interfaces in our emotional and social life.
- ➔ Automatic analysis of facial gestures is rapidly becoming an area of interest in multi-modal human-computer interaction.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Introduction

9 July, 2008  
SSIP '09

- ➔ Faces are our interfaces in our emotional and social life.
- ➔ Automatic analysis of facial gestures is rapidly becoming an area of interest in multi-modal human-computer interaction.
- ➔ Basic goal of this area of research is a human-like description of shown facial expression.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Introduction

9 July, 2008  
SSIP '09

➔ The solution of this problem can be based on the idea of some face detection approaches.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM





# Related Research Topics

9 July, 2008  
SSIP'09

➔ Face detection (one face/image)

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Related Research Topics

9 July, 2008  
SSIP'09

- ➔ Face detection (one face/image)
- ➔ Face localization (more faces/image)

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Related Research Topics

9 July, 2008  
SSIP '09

- ➔ Face detection (one face/image)
- ➔ Face localization (more faces/image)
- ➔ Facial feature detection (eyes, mouth, etc.)

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Related Research Topics

9 July, 2008  
SSIP'09

- ➔ Face detection (one face/image)
- ➔ Face localization (more faces/image)
- ➔ Facial feature detection (eyes, mouth, etc.)
- ➔ Facial expression recognition

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Related Research Topics

9 July,2008  
SSIP'09

- ➔ Face detection (one face/image)
- ➔ Face localization (more faces/image)
- ➔ Facial feature detection (eyes, mouth, etc.)
- ➔ Facial expression recognition
- ➔ Face recognition, face identification

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Related Research Topics

9 July,2008  
SSIP'09

- ➔ Face detection (one face/image)
- ➔ Face localization (more faces/image)
- ➔ Facial feature detection (eyes, mouth, etc.)
- ➔ Facial expression recognition
- ➔ Face recognition, face identification
- ➔ Face tracking

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Problems of the Face Detection

9 July,2008  
SSIP'09

➔ **Pose:** The images of a face vary due to the relative camera-face pose.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Problems of the Face Detection

9 July, 2008  
SSIP '09

- ➔ **Pose:** The images of a face vary due to the relative camera-face pose.
- ➔ **Presence or absence** of structural components (beards, mustaches, glasses etc.).

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM





# Problems of the Face Detection

9 July,2008  
SSIP'09

- ➔ **Pose:** The images of a face vary due to the relative camera-face pose.
- ➔ **Presence or absence** of structural components (beards, mustaches, glasses etc.).
- ➔ **Facial expression:** The appearance of faces are directly affected by the facial expression.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Problems of the Face Detection

9 July,2008  
SSIP'09

➔ **Occlusion:** Faces may be partially occluded by other objects.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Problems of the Face Detection

9 July,2008  
SSIP'09

- ➔ **Occlusion:** Faces may be partially occluded by other objects.
- ➔ **Image orientation:** Face images vary for different rotations about the optical axis of the camera.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Problems of the Face Detection

9 July,2008  
SSIP'09

- ➔ **Occlusion:** Faces may be partially occluded by other objects.
- ➔ **Image orientation:** Face images vary for different rotations about the optical axis of the camera.
- ➔ **Imaging conditions** (lighting, background, camera characteristics).

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Face Detection in a Singe Image

9 July,2008  
SSIP'09

➔ Knowledge-based methods (G. Yang and T.S. Huang, 1994).

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Face Detection in a Singe Image

9 July,2008  
SSIP'09

- ➔ Knowledge-based methods (G. Yang and T.S. Huang, 1994).
- ➔ Feature invariant approaches (T. K. Leung, M. C. Burl, and P. Perona, 1995), (K. C. Yow and R. Cipolla, 1996).

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Face Detection in a Single Image

9 July, 2008  
SSIP'09

- ➔ Template matching methods (A. Lanitis, C. J. Taylor, and T. F. Cootes, 1995).

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Face Detection in a Single Image

9 July, 2008  
SSIP'09

- ➔ Template matching methods (A. Lanitis, C. J. Taylor, and T. F. Cootes, 1995).
- ➔ Appearance-based methods (E. Osuna, R. Freund, and F. Girosi, 1997), (A. Fazeekas, C. Kotropoulos, I. Pitas, 2002).

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM





# Face Detection

9 July, 2008  
SSIP'09

➔ Scanning of the picture by a running window in a multiresolution pyramid.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Face Detection

9 July,2008  
SSIP'09

- ➔ Scanning of the picture by a running window in a multiresolution pyramid.
- ➔ Normalize of the window.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Face Detection

9 July, 2008  
SSIP'09

- ➔ Scanning of the picture by a running window in a multiresolution pyramid.
- ➔ Normalize of the window.
- ➔ Hide some parts of the face.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Face Detection

9 July,2008  
SSIP'09

- ➔ Scanning of the picture by a running window in a multiresolution pyramid.
- ➔ Normalize of the window.
- ➔ Hide some parts of the face.
- ➔ Normalize of the local variance of the brightness on the picture.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Face Detection

9 July, 2008  
SSIP '09

➔ Equalization of the histogram.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Face Detection

9 July, 2008  
SSIP'09

- ➔ Equalization of the histogram.
- ➔ Localization of the face (decision).

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Face Gesture Recognition

9 July, 2008  
SSIP'09

➔ Let us consider a set of the facial pictures.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Face Gesture Recognition

9 July, 2008  
SSIP'09

- ➔ Let us consider a set of the facial pictures.
- ➔ Let us set up a finite system of some features related the pictures.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM





# Face Gesture Recognition

9 July, 2008  
SSIP'09

- ➔ Let us consider a set of the facial pictures.
- ➔ Let us set up a finite system of some features related the pictures.
- ➔ It is known any pictures is related to only one class:

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Face Gesture Recognition

9 July, 2008  
SSIP'09

- ➔ Let us consider a set of the facial pictures.
- ➔ Let us set up a finite system of some features related the pictures.
- ➔ It is known any pictures is related to only one class: **face with the given gesture,**

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Face Gesture Recognition

9 July, 2008  
SSIP'09

- ➔ Let us consider a set of the facial pictures.
- ➔ Let us set up a finite system of some features related the pictures.
- ➔ It is known any pictures is related to only one class: face with the given gesture, face without the given gesture.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Face Gesture Recognition

9 July, 2008  
SSIP'09

➔ The problem to find a method to determine the class of the examined picture.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Face Gesture Recognition

9 July, 2008  
SSIP '09

- ➔ The problem to find a method to determine the class of the examined picture.
- ➔ One possible way to solve this problem: Support Vector Machine.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Experimental Results

9 July,2008  
SSIP'09

➔ For all experiments the package SVMLight developed by T. Joachims was used. For complete test, several routines have been added to the original toolbox.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Experimental Results

9 July, 2008  
SSIP '09

- ➔ For all experiments the package SVMLight developed by T. Joachims was used. For complete test, several routines have been added to the original toolbox.
- ➔ The database recorded by our institute was used.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Experimental Results

9 July, 2008  
SSIP '09

- ➔ Training set of 40 images (20 faces with the given gesture, 20 faces without the given gesture.).

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM





# Experimental Results

9 July, 2008  
SSIP '09

- ➔ Training set of 40 images (20 faces with the given gesture, 20 faces without the given gesture.).
- ➔ All images are recorded in 256 grey levels.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Experimental Results

9 July, 2008  
SSIP'09

- ➔ Training set of 40 images (20 faces with the given gesture, 20 faces without the given gesture.).
- ➔ All images are recorded in 256 grey levels.
- ➔ They are of dimension  $640 \times 480$ .

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Experimental Results

9 July, 2008  
SSIP'09

➔ The procedure for collecting face patterns is as follows.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Experimental Results

9 July, 2008  
SSIP'09

- ➔ The procedure for collecting face patterns is as follows.
- ➔ A rectangle part of dimension  $256 \times 320$  pixels has been manually determined that includes the actual face.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Experimental Results

9 July, 2008  
SSIP'09

➔ This area has been subsampled four times. At each subsampling, non-overlapping regions of  $2 \times 2$  pixels are replaced by their average.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Experimental Results

9 July, 2008  
SSIP'09

- ➔ This area has been subsampled four times. At each subsampling, non-overlapping regions of  $2 \times 2$  pixels are replaced by their average.
- ➔ The training patterns of dimension  $16 \times 20$  are built.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Experimental Results

9 July, 2008  
SSIP'09

➔ The class label +1 has been appended to each pattern.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Experimental Results

9 July, 2008  
SSIP'09

- ➔ The class label  $+1$  has been appended to each pattern.
- ➔ Similarly, 20 non-face patterns have been collected from images in the same way, and labeled  $-1$ .

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM





# Facial Gesture Database

9 July, 2008  
SSIP '09



Surprising face



Smiling face



Sad face



Angry face

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Classification Error

9 July,2008  
SSIP'09

Angry	Happy	Sad	Serial	Suprised
22.4%	10.3%	11.8%	9.4%	18.9%

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Examples

9 July, 2008  
SSIP '09



MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



















# Support Vector Machine

9 July, 2008  
SSIP'09

➔ Statistical learning from examples aims at selecting from a given set of functions  $\{f_\alpha(\mathbf{x}) \mid \alpha \in \Lambda\}$ , the one which predicts best the correct response.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Support Vector Machine

9 July, 2008  
SSIP'09

➔ This selection is based on the observation of  $l$  pairs that build the **training set**:

$$(\mathbf{x}_1, y_1), \dots, (\mathbf{x}_l, y_l), \quad \mathbf{x}_i \in \mathbb{R}^m, y_i \in \{+1, -1\}$$

which contains input vectors  $\mathbf{x}_i$  and the associated ground "truth" given by an external supervisor.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Support Vector Machine

9 July, 2008  
SSIP'09

➔ This selection is based on the observation of  $l$  pairs that build the **training set**:

$$(\mathbf{x}_1, y_1), \dots, (\mathbf{x}_l, y_l), \quad \mathbf{x}_i \in \mathbb{R}^m, y_i \in \{+1, -1\}$$

which contains input vectors  $\mathbf{x}_i$  and the associated ground "truth" given by an external supervisor.

➔ Let the response of the learning machine  $f_\alpha(\mathbf{x})$  belongs to a set of **indicator functions**.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Support Vector Machine

9 July, 2008  
SSIP'09

➔ If we define the **loss-function**:

$$L(y, f_{\alpha}(\mathbf{x})) = \begin{cases} 0, & \text{if } y = f_{\alpha}(\mathbf{x}), \\ 1, & \text{if } y \neq f_{\alpha}(\mathbf{x}). \end{cases}$$

The expected value of the loss is given by:

$$R(\alpha) = \int L(y, f_{\alpha}(\mathbf{x}))p(\mathbf{x}, y)d\mathbf{x}dy,$$

where  $p(\mathbf{x}, y)$  is the joint probability density function of random variables  $\mathbf{x}$  and  $y$ .

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Support Vector Machine

9 July, 2008  
SSIP'09

➔ We would like to find the function  $f_{\alpha_0}(\mathbf{x})$  which minimizes the risk function  $R(\alpha)$ .

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Support Vector Machine

9 July, 2008  
SSIP'09

- ➔ We would like to find the function  $f_{\alpha_0}(\mathbf{x})$  which minimizes the risk function  $R(\alpha)$ .
- ➔ The basic idea of SVM to construct the optimal separating hyperplane.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM





# Support Vector Machine

9 July, 2008  
SSIP'09

➔ Suppose that the training data can be separated by a hyperplane,  $f_{\alpha}(\mathbf{x}) = \alpha^T \mathbf{x} + b = 0$ , such that:

$$y_i(\alpha^T \mathbf{x}_i + b) \geq 1, \quad i = 1, 2, \dots, l$$

where  $\alpha$  is the normal to the hyperplane.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Support Vector Machine

9 July, 2008  
SSIP'09

- ➔ Suppose that the training data can be separated by a hyperplane,  $f_{\alpha}(\mathbf{x}) = \alpha^T \mathbf{x} + b = 0$ , such that:

$$y_i(\alpha^T \mathbf{x}_i + b) \geq 1, \quad i = 1, 2, \dots, l$$

where  $\alpha$  is the normal to the hyperplane.

- ➔ For the linearly separable case, SVM simply seeks for the **separating hyperplane** with the largest margin.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Support Vector Machine

9 July, 2008  
SSIP'09

➔ For linearly nonseparable data, by mapping the input vectors, which are the elements of the training set, into a high-dimensional feature space through so-called **kernel function**.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



# Support Vector Machine

9 July, 2008  
SSIP'09

- ➔ For linearly nonseparable data, by mapping the input vectors, which are the elements of the training set, into a high-dimensional feature space through so-called **kernel function**.
- ➔ We construct the optimal separating hyperplane in the feature space to get a binary decision.

MMHCI

Turk 2

Face detection

Face gesture

Examples

SVM



9 July,2008  
SSIP'09

Thank you for your attention!