

# APPLIANCE OF MATHEMATICS AND INFORMATIC IN RADIOLOGY

- Mathematical principles **basic** for proceedings imaging
- X ray beam, ultrasound waves and magnetic fields

## CONVENTIONAL RADIOLOGY

- Image acquired after absorption of X ray beam in the object. Attenuated X ray beam expose photo emulsion and processed



## TASK FOR MATHEMATICS:

- Measure of distance – film -> object important because ( exponential attenuation- total X ray beam doses decrease in a half, with  $x^2$  of distance
- Calculation of kV and mA (depend of constitution of the patient)



## SIMPLE MATHEMATICAL METHODES IN CONVENTIONAL RADIOLOGY

Measuring of the size of organs and pathological changes

- Describe size, shape, relations, length...

Klasifikacija	Opis	Merenje	Značajka	Lokalizacija	Napomena
1	...	...	...	...	...
2	...	...	...	...	...
3	...	...	...	...	...
4	...	...	...	...	...
5	...	...	...	...	...
6	...	...	...	...	...
7	...	...	...	...	...
8	...	...	...	...	...
9	...	...	...	...	...
10	...	...	...	...	...
11	...	...	...	...	...
12	...	...	...	...	...
13	...	...	...	...	...
14	...	...	...	...	...
15	...	...	...	...	...
16	...	...	...	...	...
17	...	...	...	...	...
18	...	...	...	...	...
19	...	...	...	...	...
20	...	...	...	...	...

## Mathematic in ULTRASOUND

- Use of ultrasound mechanical waves in originate of image
- Transducer, different frequencies,
- Acoustic impedance = different tissue  $\times$  speed of sound in material
- Degree of attenuation
- Spatial resolution



Type of US image:

- **One dimensional**  
A-mod (amplitude – mathematical function)  
M mod ( time motion )
- **Two dimensional**  
B mode image – grey scale  
(white = fibrous tissue, gray= soft tissue / fluid)
- **4D** beside 3D one more dimension...TIME



## Mathematic in INTERVENTIONAL ULTRASOUND

Measuring the size of organs, area, relations, angle for needle and catheters, depth...



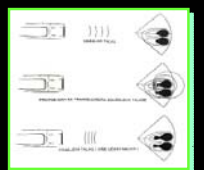
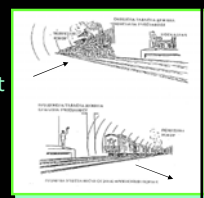
## DOPPLER EFFECT

- Psychic Johan Cristian Doppler 1842.
- DOPLER US – based on doppler effect  
Change of freq. of sound, light or other waves caused by moving source or object (red blood cells...)

HOW can we evaluate blod flow ?

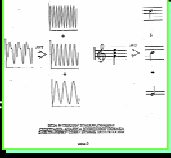
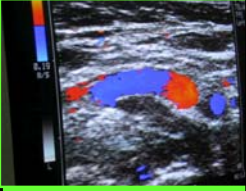

$$V_x \cos \theta = \frac{C_x F_p}{2x F_o}$$

- $V$  flow
- $C$  speed of US in tissue (1540 m/s)
- $F_p$  frequency change
- $F_o$  frequency of US
- $\cos \theta$  cosinus angle  $\theta$  between US wave and blood flow



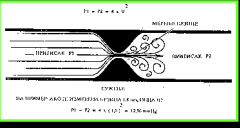
- RBC move with different speed → different freq.
- Mathematics analyse use Fast Fourier transformation FFT
- Result is spectral analyse of Doppler change give graphical presentation of blood flow

**COLOR FLOW DOPPLER**  
Different color for direction of movement  
**TO transducer** and **FROM transducer**  
Volume, index of the resistance...

**DOPPLER US diagnostic of blood vessel**



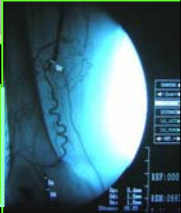
- Stenosis and occlusion result in decrease of the fluid pressure = gradient pressure
- Before occlusion fluid have higher pressure
- Link between pressure gradient and speed measured after stenosis is simplified by Bernoulli's function:

$$P_1 - P_2 = 4 \times V^2$$


- US equipment have great technical possibility for quality processing of the image (index of resistance)
- From simple mathematics measuring to the most complicated mathematics image processing




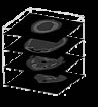

**Appliance of Mathematics in Angio Rooms**

- Positioning of examination table/patients
- Angles of tube rotation, magnification...
- Bloodflow, pressure, time of contrast appliance
- Measurements of perceived changes and mathematical calculation of narrowed space...

**Mathematics and CT (Computerized tomography)**

- Since highly sophisticated software packages and computers are developed, it is possible to process a large amount of received data from the whole-body-scan with classical X-rays, from more angles at the same time or in a short period of time
- The picture is formed from received scanned image slices of body in form of "pixel" (2D) and "voxel" (3D)

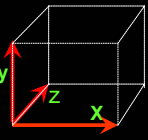
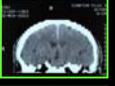
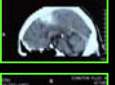
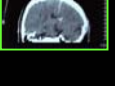

**Mathematics and CT (Computerized tomography)**

Possibility of tissue measurement (Hounsfield units HU - gray/white scale)

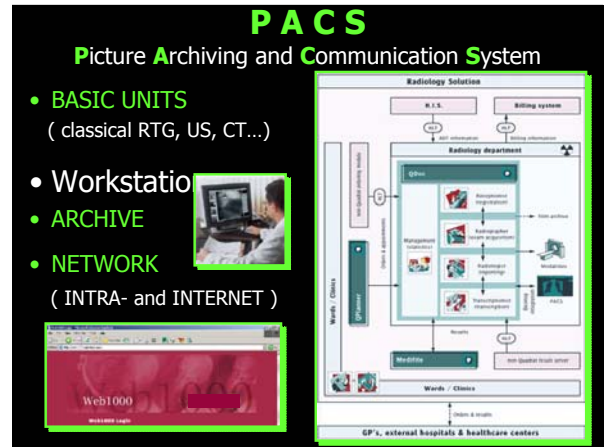
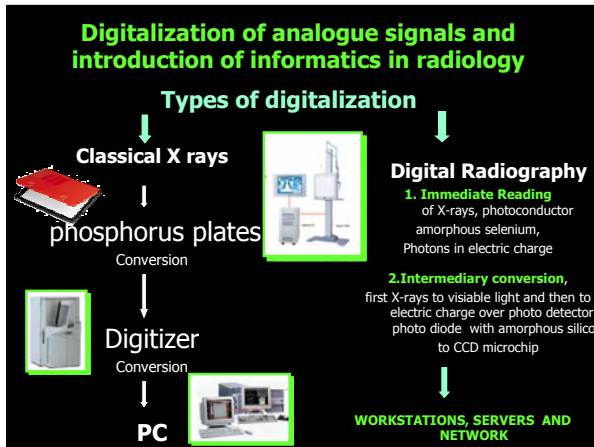
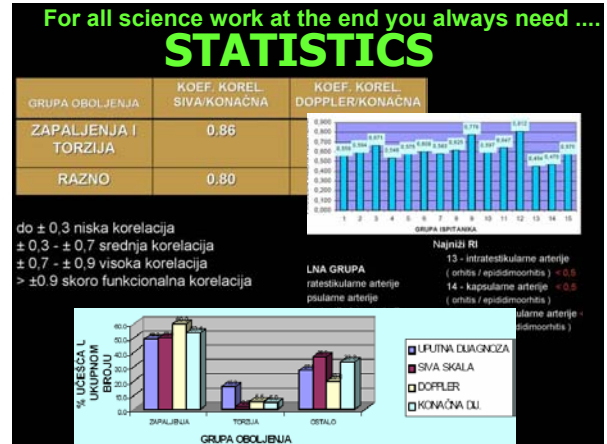
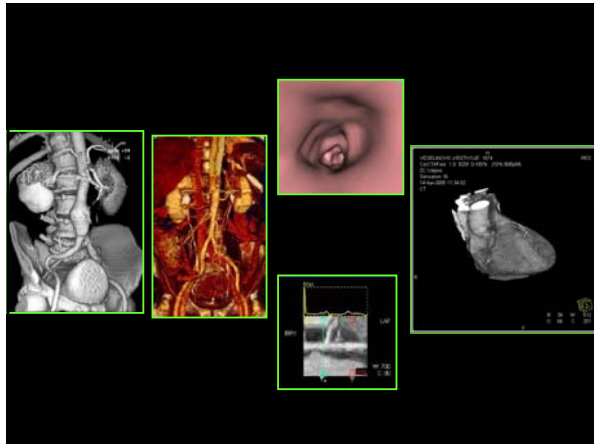
-1000 = air  
0 = water  
+1000 = bone

Multiplanar reconstruction

- coronary reconstruction
- sagittal reconstruction
- Paraxial reconstruction

- **Conventional scanners** with one rotation of the X-ray tube around the object and move for **one layer depth**- sequent mode
- Helical- one spiral around patient
- Next generation of **multislice** CT scanners (2, 4... 14... 64 )
- Collected data of scanned volumen
- Edited in post processing with different software packages, which enables 2D and 3D view
- 3D picture reconstruction, **Shaded Surface Display**, **Volume Rendering**, **Vessel View**, **Fly Through**...
- CT-angio and CT coronography, CT virtual colonography...



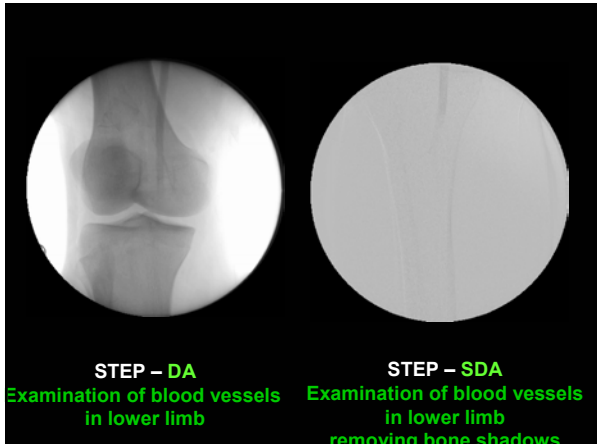
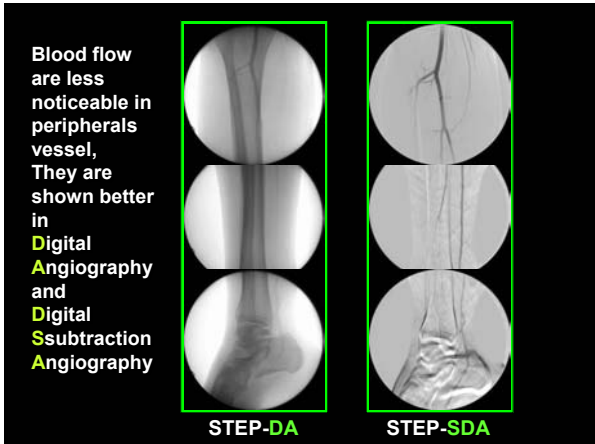
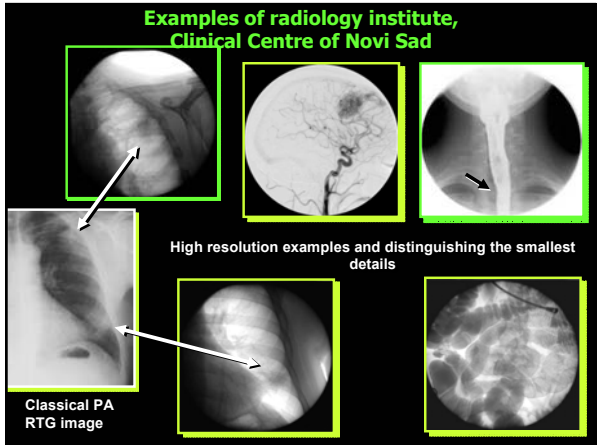
- ADVANTAGES OF PACS**
- Reduce pictures
  - Less radiation exposure
  - Real time picture availability on a workstation
  - Cost saving on material used in examination
  - No more darkroom, "oops we let the sunshine in..."

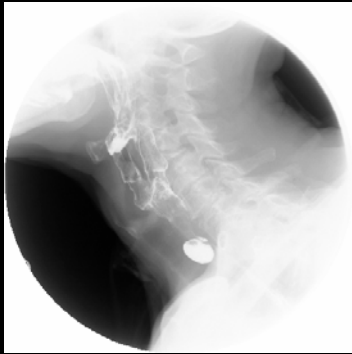
- Excellent picture **quality**, no more "repeat softer or harder"
- Advanced, less dangerous work condition – Less radiation **exposure** !
- Instant picture availability , **no more "please wait , developing..."**

- Advantage of **digital archiving**
  - no need for large rooms, or cupboards...
  - losing of images reduced
  - query after many years is very simple
- **Comparison** with other images is **easier** then ever
- **Additional** image **editing** possible (changing brightness and contrast, enlargement, measurement...)

- **Access** to images in any part of hospital/department is possible...
- Case introduction and science works ease
- Better treatment in emergency cases – thanks to **teleradiology**

- ### FLAWS OF PACS
- Installation costs too high (?)
  - Errors and damages on main parts ( SERVER, READER...) CAUSES BLOCKING OR LOSS OF DATA
  - CHANGING HABBITS ?!
  - NEED FOR EDUCATION AND HIRING NEW EXPERTS

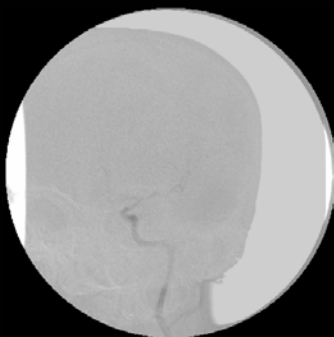




Diverticle of esophagus (saccular expansion of wall)  
Act of swallowing in real time

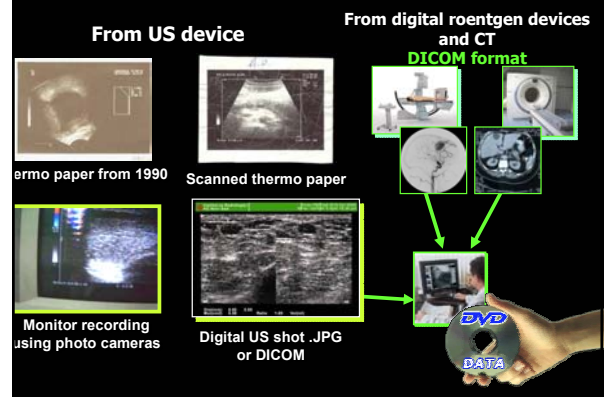


AV - MALFORMATION  
(pathologically branched blood vessels of the brain)



R-DSA = ROTATION DIGITAL SUBTRACION ANGIOGRAPHY  
Head blood vessels examination in real time removing bone mask  
Rotating the tube for 15-900

### Improvements in image archiving



### RESULTS INSTITUTE OF RADIOLOGY, KC Novi Sad

- **70% of patients** examined with digitalized method the *checkup quality is greatly enhanced* and the period of examination is reduced (also the exposure to radiation of patient, technician i radiologist is shorter).
- **New types of exams** are introduced (digital subtraction angiography) quality and *sensibility* of old methods are also improved.
- With digital technique *reediting* of image is possible
- **„Post processing“**, changes of contrast, brightness, measurement ... on all examined patients, additional *tracking of image* dynamics in real time, while on classical rtg devices is not possible.
- **Additional improvements** in quality are achieved, also in image *archiving*, printed on standard thermo paper of ultrasound devices, in comparison to new digital scanning.
- **CT scanners** are now connected with **PCs**, additional examination, editing and archiving on disc media.

### CONCLUSION:

- **Mathematics** is the basic tool in achieving and editing analogue and digital radiological images
  - **Quick** examinations and improved quality, pace and reliability of diagnostics itself.
  - **Cost-effectiveness** in material and time, exposure to radiation is reduced for everyone, patient, radiologist and technician.
  - Additional **editing options**, **archiving** and **interchanges** enable consulting on distance (teleradiology) and appliance in education.
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